

Hyperon-nucleon interaction in few- and many-body systems

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- 4 Neutron stars
- 5 Strangeness $S=-1$ dibaryon
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Interaction of strange baryons

- ΛN and ΣN scattering
 - Role of **SU(3)** flavor symmetry
- **H dibaryon**
 - Jaffe (1977) → **deeply bound 6-quark state** with $I = 0, J = 0, S = -2$
 - **many** experimental **searches** but **no convincing signal**
 - Lattice QCD (2010) → **evidence for a bound H dibaryon** ($\Lambda\Lambda$)
- Few-body systems with **hyperons**: ${}^3_{\Lambda}\text{H}, {}^4_{\Lambda}\text{H}, {}^4_{\Lambda}\text{He}, \dots$
 - Role of **three-body forces**
 - large **charge symmetry breaking** ${}^4_{\Lambda}\text{H} \leftrightarrow {}^4_{\Lambda}\text{He}$
- (Λ, Σ) **hypernuclei** and **hyperons** in **nuclear matter**
 - very small spin-orbit splitting: **weak spin-orbit force**
 - existence of Ξ **hypernuclei**
 - repulsive** Σ nuclear potential
- implications for **astrophysics**
 - **stability/size** of **neutron stars**
 - softening** of **equation of state** (**hyperon puzzle**)
 - hyperon** stars

BB interaction in chiral effective field theory

Baryon-baryon interaction in $SU(3)$ χ EFT à la Weinberg (1990) [up to NLO]

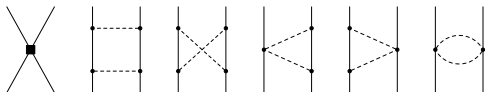
Advantages:

- Power counting
systematic improvement by going to higher order
- Possibility to derive two- and three-baryon forces and external current operators in a consistent way
- degrees of freedom: octet baryons (N, Λ, Σ, Ξ), pseudoscalar mesons (π, K, η)
- pseudoscalar-meson exchanges (V^{OBE}, V^{TBE})
- contact terms – represent unresolved short-distance dynamics (V^{CT})

LO :



NLO :



LO: H. Polinder, J.H., U.-G. Meißner, NPA 779 (2006) 244

NLO: J.H., N. Kaiser, U.-G. Meißner, A. Nogga, S. Petschauer, W. Weise, NPA 915 (2013) 24



Pseudoscalar-meson exchange

$$V_{B_1 B_2 \rightarrow B'_1 B'_2}^{OBE} = -f_{B_1 B'_1 P} f_{B_2 B'_2 P} \frac{(\vec{\sigma}_1 \cdot \vec{q})(\vec{\sigma}_2 \cdot \vec{q})}{\vec{q}^2 + m_P^2}, \quad \vec{q} = \vec{p}' - \vec{p}$$

$$V_{B_1 B_2 \rightarrow B'_1 B'_2}^{TBE} = \dots$$

$f_{B_1 B'_1 P}$... coupling constants fulfil standard **SU(3)** relations

m_P ... mass of the **exchanged pseudoscalar meson**

SU(3) symmetry breaking due to the **mass splitting** of the **ps mesons**
 ($m_\pi = 138.0$ MeV, $m_K = 495.7$ MeV, $m_\eta = 547.3$ MeV)

Contact interaction V^{CT} - partial-wave projected

$$V(^1S_0) = \tilde{C}_{1S_0} + C_{1S_0}(p^2 + p'^2)$$

$$V(^3S_1) = \tilde{C}_{3S_1} + C_{3S_1}(p^2 + p'^2)$$

$$V(\alpha) = C_\alpha p p' \quad \alpha \hat{=} ^1P_1, ^3P_0, ^3P_1, ^3P_2$$

$$V(^3D_1 \leftrightarrow ^3S_1) = C_{3S_1-3D_1} p'^2, C_{3S_1-3D_1} p^2$$

$$V(^1P_1 \leftrightarrow ^3P_1) = C_{1P_1-3P_1} p p'$$

\tilde{C} 's, C 's ... low-energy constants (**LECs**) ... to be **fixed** from **fit to data**

$SU(3)$ structure of contact terms for BB

$SU(3)$ structure for scattering of two octet baryons \rightarrow

$$8 \otimes 8 = 1 \oplus 8_a \oplus 8_s \oplus 10^* \oplus 10 \oplus 27$$

BB interaction can be given in terms of LECs corresponding to the $SU(3)_f$ irreducible representations: C^1 , C^{8_a} , C^{8_s} , C^{10^*} , C^{10} , C^{27}

	Channel	l	V_α	V_β	$V_{\beta \rightarrow \alpha}$
$S = 0$	$NN \rightarrow NN$	0	–	$C_\beta^{10^*}$	–
	$NN \rightarrow NN$	1	C_α^{27}	–	–
$S = -1$	$\Lambda N \rightarrow \Lambda N$	$\frac{1}{2}$	$\frac{1}{10} (9C_\alpha^{27} + C_\alpha^{8_s})$	$\frac{1}{2} (C_\beta^{8_a} + C_\beta^{10^*})$	$-C^{8_{sa}}$
	$\Lambda N \rightarrow \Sigma N$	$\frac{1}{2}$	$\frac{3}{10} (-C_\alpha^{27} + C_\alpha^{8_s})$	$\frac{1}{2} (-C_\beta^{8_a} + C_\beta^{10^*})$	$-3C^{8_{sa}}$ $C^{8_{sa}}$
	$\Sigma N \rightarrow \Sigma N$	$\frac{1}{2}$	$\frac{1}{10} (C_\alpha^{27} + 9C_\alpha^{8_s})$	$\frac{1}{2} (C_\beta^{8_a} + C_\beta^{10^*})$	$3C^{8_{sa}}$
	$\Sigma N \rightarrow \Sigma N$	$\frac{3}{2}$	C_α^{27}	C_β^{10}	–

$$\alpha = {}^1S_0, {}^3P_0, {}^3P_1, {}^3P_2, \quad \beta = {}^3S_1, {}^3S_1 - {}^3D_1, {}^1P_1$$

No. of contact terms: LO: 2 (NN) + 3 (YN) + 1 (YY)

NLO: 7 (NN) + 11 (YN) + 4 (YY)

NB: $\Lambda N, \Sigma N \rightarrow 10$ LECs in S waves relevant at low energies

Coupled channels Lippmann-Schwinger Equation

$$T_{\rho' \rho}^{\nu' \nu, J}(p', p) = V_{\rho' \rho}^{\nu' \nu, J}(p', p) + \sum_{\rho'', \nu''} \int_0^\infty \frac{dp'' p''^2}{(2\pi)^3} V_{\rho' \rho''}^{\nu' \nu'', J}(p', p'') \frac{2\mu_{\rho''}}{p^2 - p''^2 + i\eta} T_{\rho'' \rho}^{\nu'' \nu, J}(p'', p)$$

$$\rho', \rho = \Lambda N, \Sigma N \quad (\Lambda\Lambda, \Xi N, \Lambda\Sigma, \Sigma\Sigma)$$

LS equation is solved for **particle channels** (in **momentum space**)

Coulomb interaction is included via the **Vincent-Phatak method**

The potential in the **LS** equation is cut off with the **regulator function**:

$$V_{\rho' \rho}^{\nu' \nu, J}(p', p) \rightarrow f^\Lambda(p') V_{\rho' \rho}^{\nu' \nu, J}(p', p) f^\Lambda(p); \quad f^\Lambda(p) = e^{-(p/\Lambda)^4}$$

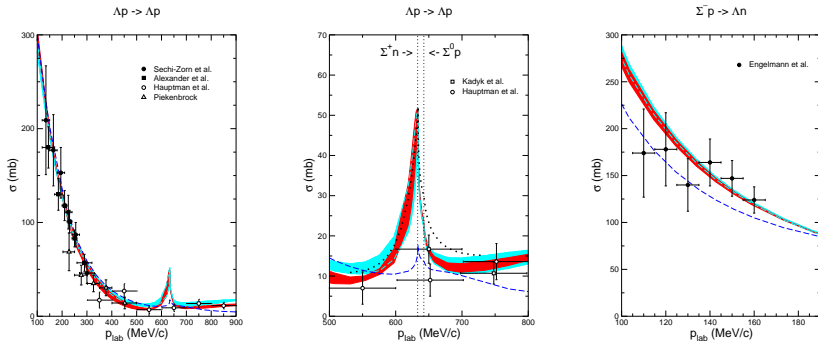
consider values $\Lambda = 500 - 650$ MeV [guided by NN , achieved χ^2]

ideally the **regulator** (Λ) dependence should be **absorbed** completely by the **LECs**

in practice there is a **residual regulator dependence** (shown by **bands** below)

- **tells us** something about the **convergence**
- **tells us** something about the **size** of **higher-order contributions**

ΥN integrated cross sections



NLO13 ... all **S-wave LECs** are fixed from a fit directly to available ΥN data

NLO19 ... consider constraints from the NN interaction within (broken) **SU(3) symmetry**

NLO13: J.H., S. Petschauer, N. Kaiser, U.-G. Meißner, A. Nogga, W. Weise, NPA 915 (2013) 24

NLO19: J.H., U.-G. Meißner, A. Nogga, EPJA 56 (2020) 91

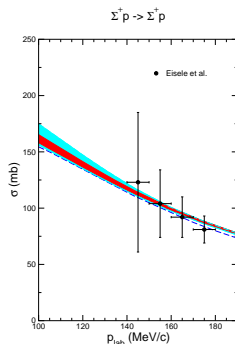
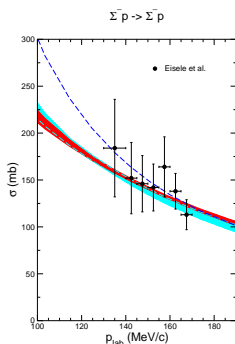
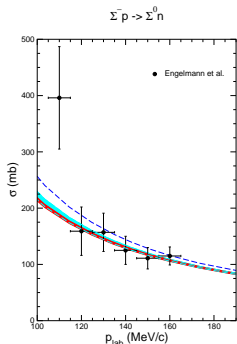
Jülich '04: J.H., U.-G. Meißner, PRC 72 (2005) 044005

Nijmegen NSC97f: T.A. Rijken et al., PRC 59 (1999) 21

data points included in the fit are represented by filled symbols!



ΥN integrated cross sections



NLO13: J.H., S. Petschauer, N. Kaiser, U.-G. Meißner, A. Nogga, W. Weise, NPA 915 (2013) 24

NLO19: J.H., U.-G. Meißner, A. Nogga, EPJA 56 (2020) 91

Jülich '04: J.H., U.-G. Meißner, PRC 72 (2005) 044005

quality of the fit – total χ^2 (36 data points):

NLO13: 15.7 ... 16.8

NLO19: 16.0 ... 18.1

Jülich '04: ≈ 22

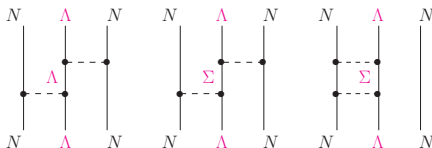
Difference between NLO13 and NLO19

Different coupling strength between the ΛN and ΣN channels ($V_{\Lambda N \leftrightarrow \Sigma N}$)

consequences for in-medium properties:

ΛN - ΣN coupling is suppressed for increasing number of nucleons

dispersive effects in few-body systems:



$$V_{\Lambda N}^{\text{eff}}(E) \approx V_{\Lambda N} + V_{\Lambda N \rightarrow \Sigma N} \frac{1}{E - H_0} V_{\Sigma N \rightarrow \Lambda N}$$

(propagator includes the energy of the spectator nucleons!)

Pauli blocking effects in nuclear matter:

$$V_{\Lambda N}^{\text{eff}}(\epsilon) \approx V_{\Lambda N} + V_{\Lambda N \rightarrow \Sigma N} \frac{Q}{\epsilon - H_0} V_{\Sigma N \rightarrow \Lambda N}$$

EFT: in consistent few- and many-body calculations, differences in the two-body potential (in the ΛN - ΣN coupling) are to be compensated by many-body forces

→ tool for estimating effects from three-body forces!

3- and many-body forces in chiral EFT (E. Epelbaum)

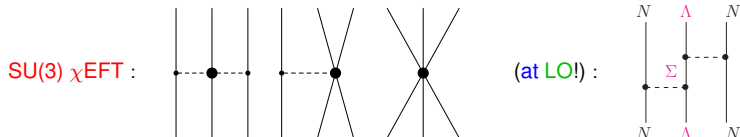
	Two-nucleon force	Three-nucleon force	Four-nucleon force
LO (Q^0)			
NLO (Q^2)			
N ² LO (Q^3)			
N ³ LO (Q^4)			

different hierarchy of 3BFs
for other counting schemes
(Hammer, Nogga, Schwenk,
Rev. Mod. Phys. 85 (2013) 197)

	pionless	chiral	chiral+ Δ
LO			
NLO			
N ² LO			

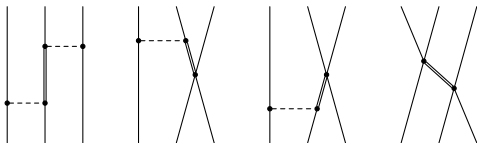
Three-body forces

- $SU(3)$ χ EFT 3BFs nominally at N^2 LO (S. Petschauer et al., PRC 93 (2016) 014001)
- not included in present (NLO) calculation!



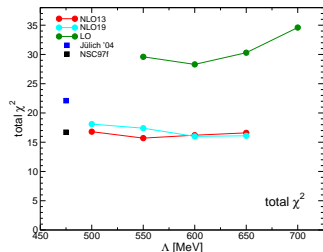
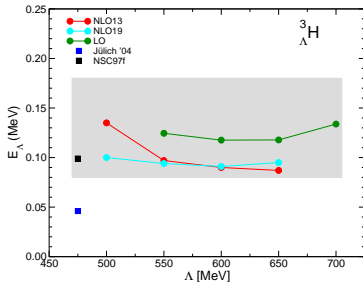
solve coupled channel (ΛN - ΣN) Faddeev-Yakubovsky equations:
 \Rightarrow ΛNN "3BF" from Σ coupling is automatically included
 remaining 3BF expected to be moderate

- ΛNN 3BF via Σ^* excitation in $SU(3)$ χ EFT with $\{10\}$ baryons (NLO)



estimate ΛNN 3BF based on the $\Sigma^*(1385)$ excitation (S. Petschauer et al., NPA 957 (2017) 347)

Hypertriton (Faddeev calculation by A. Nogga)



(separation energy $E_\Lambda = B_\Lambda - B_d = 0.13 \pm 0.05$ MeV (M. Jurič et al., 1973))

- $B_\Lambda(^3\Lambda\text{H})$ is used as additional constraint in EFT and Jülich '04
 Λp data alone do not allow to disentangle 1S_0 (s) and 3S_1 (t) contributions
- cutoff variation:

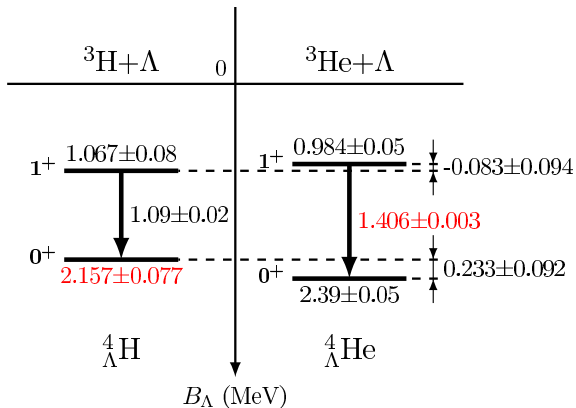
* $NNN \rightarrow$ is lower bound for magnitude of higher order contributions

* ΛNN - correlation with χ^2 of YN interaction

\Rightarrow effect of three-body forces small?

◆ STAR (J. Adam et al., Nature Phys. 16 (2020) 409) ($^3\Lambda\text{H} + ^3\Lambda\bar{\text{H}}$): $0.41 \pm 0.12 \pm 0.11$ MeV !?

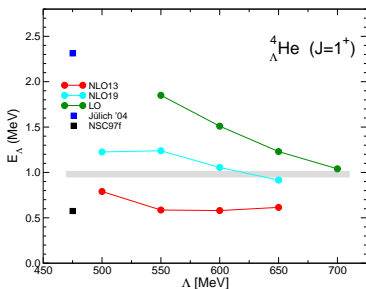
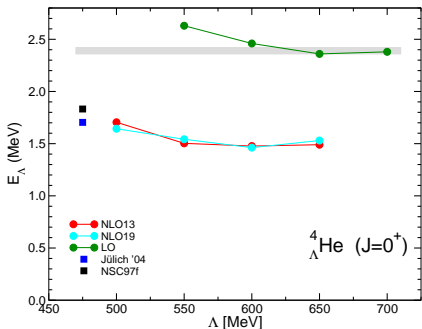
(NN potential: SMS N⁴LO+ (450) (P. Reinert et al., EPJA 54 (2018) 86))



large CSB in 0^+ ($\Delta \approx 233$ keV), small CSB in 1^+ ($\Delta \approx -83$ keV)

F. Schulz et al. [A1 Collaboration] (2016), T.O. Yamamoto et al. [J-PARC E13 Collaboration] (2015)

$^4_\Lambda\text{He}$ results (Faddeev-Yakubovsky – by A. Nogga)



- LO: unexpected small cutoff dependence in 0^+ result
 - NLO: underbinding in χEFT and for phenomenological potentials
 - possible effects of long ranged three-body forces?
- (no CSB in χEFT YN potentials!)

Estimation of 3BFs based on NLO results

● ${}^3_{\Lambda}\text{H}$

(a) cutoff variation: ΔE_{Λ} (3BF) ≤ 50 keV

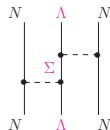
(b) "3BF" from ΛN - ΣN coupling:

switch off ΛN - ΣN coupling

in Faddeev-Yakubovsky equations:

ΔE_{Λ} (3BF) ≈ 10 keV

expect similar/smaller ΔE_{Λ} from Σ^* (1385) excitation



(c) ${}^3\text{H}$: $3\text{NF} \sim Q^3 |\langle V_{NN} \rangle|_{3\text{H}} \sim 650$ keV

($|\langle V_{NN} \rangle|_{3\text{H}} \sim 50$ MeV; $Q \sim m_{\pi}/\Lambda_b$; $\Lambda_b \simeq 600$ MeV)

${}^3_{\Lambda}\text{H}$: $|\langle V_{\Lambda N} \rangle|_{3\text{H}} \sim 3$ MeV $\rightarrow \Delta E_{\Lambda}$ (3BF) $\approx Q^3 |\langle V_{\Lambda N} \rangle|_{3\text{H}} \simeq 40$ keV

● ${}^4_{\Lambda}\text{H}$, ${}^4_{\Lambda}\text{He}$

(a) cutoff variation: ΔE_{Λ} (3BF) ≈ 200 keV (0^+) and ≈ 300 keV (1^+)

(b) "3BF" from ΛN - ΣN coupling:

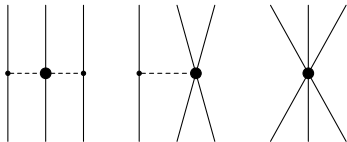
ΔE_{Λ} (3BF) $\approx 230 - 340$ keV (0^+), $\approx 150 - 180$ keV (1^+)

${}^3_{\Lambda}\text{H}$ and ${}^4_{\Lambda}\text{H}(\text{He})$ calculations with explicit inclusion of 3BFs are planned for the future

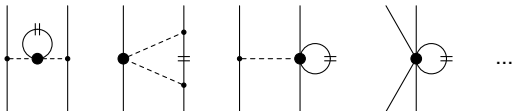
density dependent effective ΛN interaction

(for application to heavy hypernuclei and hyperons in infinite nuclear matter)

three-body force:



⇒ density dependent effective ΛN interaction:



close two baryon lines by sum over occupied states within the Fermi sea
arising 3BF LECs can be constrained by resonance saturation (via decuplet baryons)
(→ 1 for ΛNN , 2 for ΣNN , ΞNN , ...)

J.W. Holt, N. Kaiser, W. Weise, PRC 81 (2010) 064009 (for NNN)

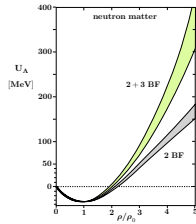
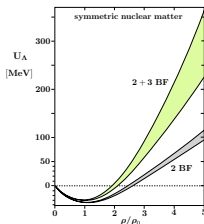
S. Petschauer et al., NPA 957 (2017) 347 (for ΛNN)

D. Gerstung et al., EPJA 56 (2020) 175 (ΛNN , ΣNN)

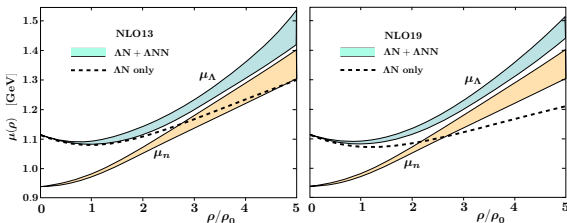
Implications for neutron stars (incl. chiral 3BF)

D. Gerstung et al.,
EPJA 56 (2020) 175
(NLO13 & NLO19; ΛNN , ΣNN)

U_Λ ... Λ single-particle potential
($U_\Lambda(\rho_0 = 0.17 \text{ fm}^{-3}) \approx -28 \dots -30 \text{ MeV}$)



Chemical potentials of the Λ hyperon (μ_Λ) and the neutron (μ_n)



$\mu_\Lambda(\rho) \leq \mu_n(\rho) \Rightarrow$ energetically favorable to replace n by Λ ($\mu_\Lambda(\rho) = M_\Lambda + U_\Lambda(\rho)$)

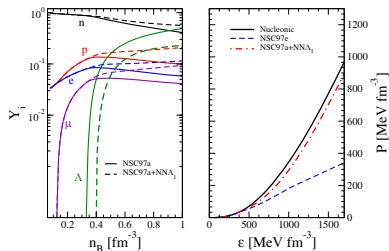
Equation-of-state becomes too soft to support $2 M_\odot$ neutron stars (“hyperon puzzle”)

Implications for neutron stars (incl. **chiral 3BF**)

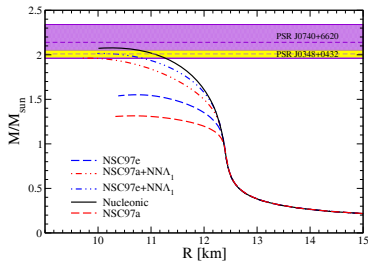
Logoteta, Vidaña, Bombaci,
EPJA 55 (2019) 207
(Nijmegen NSC97 potentials)

Composition and **EoS**
of neutron star matter

($n_B \equiv \rho$)

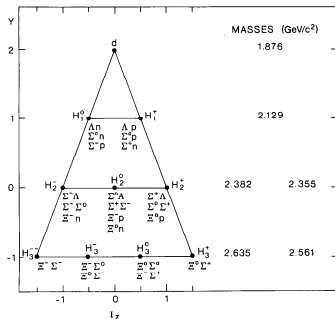


Mass-radius relation without and with **chiral ΛNN** force



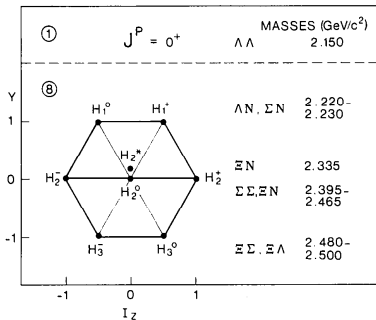
	$M_{max}(M_{\odot})$	R (km)	n_c (fm^{-3})
Nucleonic	2.08	10.26	1.15
NSC97a	1.31	10.60	1.40
NSC97a+NNA ₁	1.96	9.80	1.30
NSC97a+NNA ₂	1.97	9.87	1.28
NSC97e	1.54	10.81	1.18
NSC97e+NNA ₁	2.01	10.10	1.20
NSC97e+NNA ₂	2.02	10.15	1.19

Strange dibaryons



R.J. Oakes, PR 131 (1963) 2239

SU(3) flavor symmetry {10*}
strange partners of the deuteron

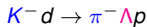
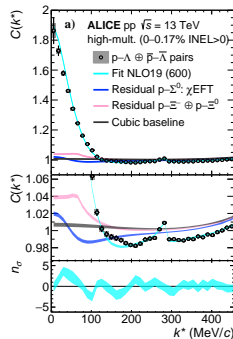
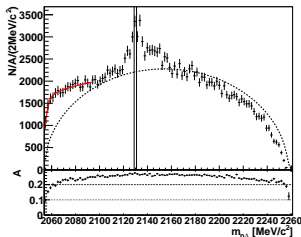
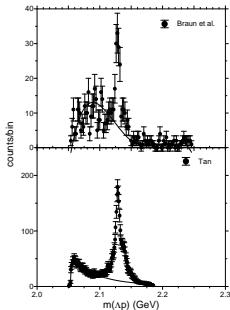


R.L. Jaffe, PRL 38 (1977) 195

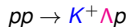
MIT quark bag model

Experimental evidence for threshold structure

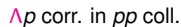
$$M_{\Sigma^+} + M_n = 2128.97 \text{ MeV} \quad M_{\Sigma^0} + M_p = 2130.87 \text{ MeV}$$



T.T. Tan, PRL 7 (1969) 395
O. Braun et al., NPB 124 (1977) 45



M. Röder et al., EPJA 49 (2013) 157



S. Acharya [ALICE Coll.],
arXiv:2104.04427

“ordinary” threshold effect? bound state? virtual state ($np \ ^1S_0$) ?

χ^2 for Σ^-p and Σ^+p data

ΛN result near ΣN threshold is primarily constrained by near-threshold

(20) Σ^-p data

reaction	NLO13				NLO19				Jülich '04	NSC97f (ND)
	500	550	600	650	500	550	600	650		
$\Sigma^-p \rightarrow \Lambda n$	3.7	3.9	4.1	4.4	4.7	4.7	4.0	4.4	8.3	3.9 (4.3)
$\Sigma^-p \rightarrow \Sigma^0 n$	6.1	5.8	5.8	5.7	5.5	5.5	6.0	5.7	6.4	6.0 (5.5)
$\Sigma^-p \rightarrow \Sigma^- p$	2.0	1.8	1.9	1.9	3.0	2.9	2.2	1.9	1.6	2.3 (3.6)
$\Sigma^+p \rightarrow \Sigma^+ p$	0.3	0.4	0.5	0.3	0.3	0.4	0.4	0.3	0.1	0.2 (0.1)
r_R	0.1	0.2	0.1	0.2	1.1	0.7	0.1	0.5	53.6	0.0 (0.9)
total χ^2	12.2	12.0	12.3	12.5	14.6	14.2	12.7	12.8	70 [16.4]	12.4 (14.4)

$$\left(r_R = \frac{1}{4} \frac{\sigma_s(\Sigma^-p \rightarrow \Sigma^0 n)}{\sigma_s(\Sigma^-p \rightarrow \Lambda n) + \sigma_s(\Sigma^-p \rightarrow \Sigma^0 n)} + \frac{3}{4} \frac{\sigma_t(\Sigma^-p \rightarrow \Sigma^0 n)}{\sigma_t(\Sigma^-p \rightarrow \Lambda n) + \sigma_t(\Sigma^-p \rightarrow \Sigma^0 n)} \right)$$

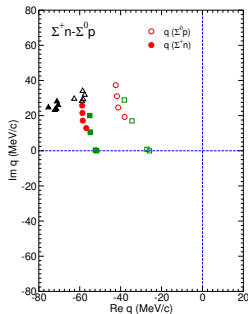
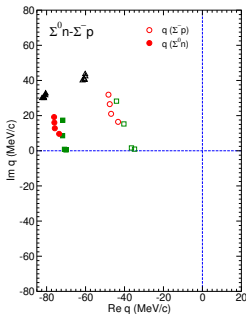
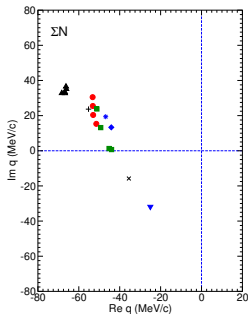
best description of near-threshold ΣN data: NLO13, NLO19 (600,650), NSC97a-f

$\Rightarrow \chi^2 = 12 - 13$

J.H., U.-G. Meißner, arXiv:2105.00836 \Rightarrow search for ΣN poles in complex plane

Poles in the complex $q_{\Sigma N}$ plane

- 2nd quadrant (sheet II, bt): unstable bound state
- 3rd quadrant (sheet IV, tb): inelastic virtual state



- NLO13
- NLO19
- ▲ Nijmegen NSC97b-f
- ▼ Jülich '04
- × Nijmegen ND (1977)

NLO13: $E = 2131.90 - i1.39 \dots 2131.25 - i3.01$ MeV

NLO19: $E = 2131.73 - i1.11 \dots 2131.35 - i0.00$ MeV

NSC97: $E = 2133.04 - i3.80 \dots 2133.79 - i3.53$ MeV

Thresholds: $\Sigma^+ n$ (2128.97) $\Sigma^0 p$ (2130.87)

⇒ bound state (dibaryon) – but above threshold!

Summary

Hyperon-nucleon interaction constructed within chiral EFT

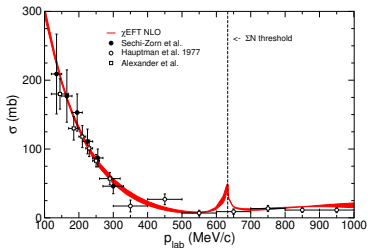
- Approach is based on a modified Weinberg power counting, analogous to applications for NN scattering
- The potential (contact terms, pseudoscalar-meson exchanges) is derived imposing $SU(3)_f$ constraints
- $S = -1$: Excellent results at next-to-leading order (NLO)
 Λp , ΣN low-energy data are reproduced with a quality comparable to phenomenological models
- $S = -1$ dibaryon: strong evidence for its existence
– but not as ideal textbook (Breit-Wigner type) resonance

Hypernuclei

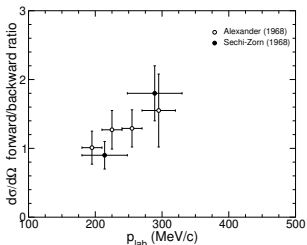
- for very light hypernuclei three-body forces should be small (${}^3_{\Lambda}\text{H}$) or moderate (${}^4_{\Lambda}\text{H}$, ${}^4_{\Lambda}\text{He}$)
needs to be quantified/confirmed by explicit inclusion of 3BFs
- ${}^5_{\Lambda}\text{He}$, etc. ... effects of three-body forces could be more significant
- Study of charge-symmetry breaking in ${}^4_{\Lambda}\text{H} - {}^4_{\Lambda}\text{He}$ is under way
- Λ hypernuclei - data with higher precision are needed to quantify 3BFs

ΛN interaction: bulk properties are known

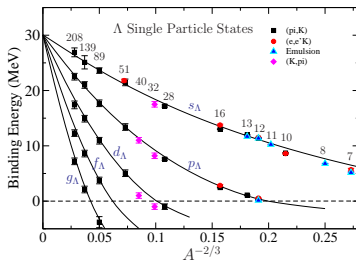
Λp cross section



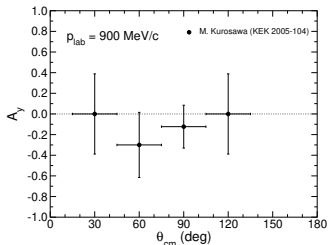
$\Lambda p \rightarrow \Lambda p$



Λ hypernuclei



$\Lambda p \rightarrow \Lambda p$



ΛN scattering lengths [fm]

	NLO13	NLO19	Jülich '04	NSC97f	experiment*
Λ [MeV]	500 ... 650	500 ... 650			
$a_s^{\Lambda p}$	-2.91 ... -2.90	-2.91 ... -2.90	-2.56	-2.51	$-1.8^{+2.3}_{-4.2}$
$a_t^{\Lambda p}$	-1.61 ... -1.51	-1.52 ... -1.40	-1.66	-1.75	$-1.6^{+1.1}_{-0.8}$
$a_s^{\Sigma^+ p}$	-3.60 ... -3.46	-3.90 ... -3.43	-4.71	-4.35	
$a_t^{\Sigma^+ p}$	0.49 ... 0.48	0.48 ... 0.42	0.29	-0.25	
χ^2	15.7 ... 16.8	16.0 ... 18.1	≈ 22	16.7	
$B(\Lambda^3\text{H})$	-2.30 ... -2.33	-2.32 ... -2.32	-2.27	-2.30	-2.354(50)

*G. Alexander et al., PR 173 (1968) 1452

Note: $B(\Lambda^3\text{H})$ is used as additional constraint in EFT and Jülich '04

Λp data alone do not allow to disentangle 1S_0 (s) and 3S_1 (t) contributions

(a , r in fm; B in MeV)

Λ and Σ in infinite nuclear matter

non-relativistic **lowest order Brueckner** theory (Bethe-Goldstone equation):

$$\langle YN | G_{YN}(\zeta) | YN \rangle = \langle YN | V | YN \rangle + \sum_{Y'N} \langle YN | V | Y'N \rangle \langle Y'N | \frac{Q}{\zeta - H_0} | Y'N \rangle \langle Y'N | G_{YN}(\zeta) | YN \rangle$$

Q ... Pauli projection operator

$$\zeta = E_Y(p_Y) + E_N(p_N)$$

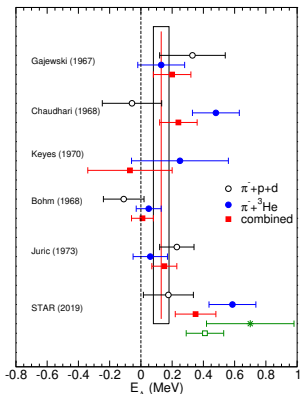
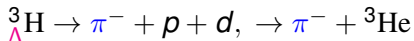
$$E_\alpha(p_\alpha) = M_\alpha + \frac{p_\alpha^2}{2M_\alpha} + U_\alpha(p_\alpha), \quad \alpha = \Lambda, \Sigma, N$$

U_α ... single-particle potential

$$U_Y(p_Y) = \int_{p_N \leq k_F} d^3 p_N \langle YN | G_{YN}(\zeta(U_Y)) | YN \rangle$$

$B_Y(\infty) = -U_Y(p_Y = 0)$ - **evaluated at saturation point of nuclear matter**

- ⇒ J.H., U.-G. Meißner, NPA 936 (2015) 29; S. Petschauer, et al., EPJA 52 (2016) 15
J.H., U.-G. Meißner, A. Nogga, EPJA 56 (2020) 91



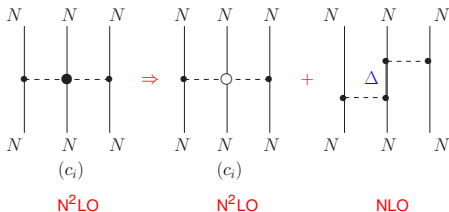
benchmark: (M. Jurič et al., 1973): 0.13 ± 0.05 MeV

STAR (J. Adam et al., Nature Phys. 16 (2020) 409) (${}^3_{\Lambda}\text{H}+{}^3\bar{\text{H}}$): $0.41 \pm 0.12 \pm 0.11$ MeV

(separation energy $E_{\Lambda} = B_{\Lambda} - B_d$)

Three-nucleon forces: Explicit inclusion of the $\Delta(1232)$

- **Explicit treatment** of the Δ (Krebs, Gasparyan, Epelbaum, PRC 98 (2018) 014003):



LECs (from πN)	c_1	c_2	c_3	c_4
Δ -less approach	-0.75	3.49	-4.77	3.34
Δ -full approach	-0.75	1.90	-1.78	1.50
Δ contribution	0	2.81	-2.81	1.40

- more **natural size** of LECs
- **better convergence** of EFT expansion (**3NF** from $\Delta(1232)$ appears at **NLO!**)
- applicability at higher energies