

Outlook Talk Status of the g-2 Problem

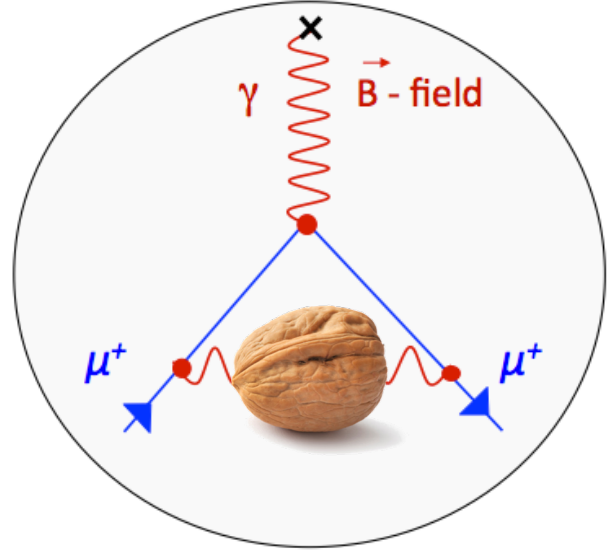
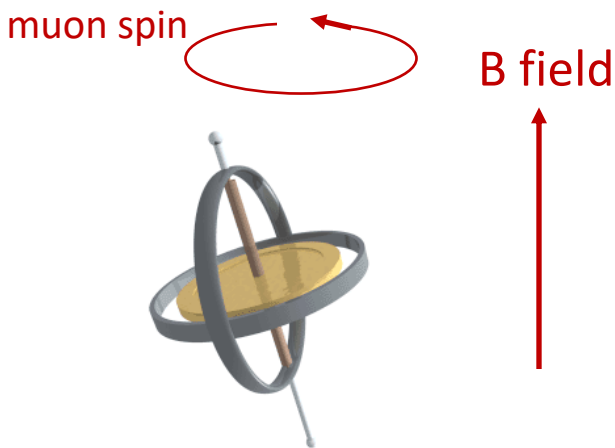


May 20, 2021
Achim Denig
Johannes Gutenberg University Mainz

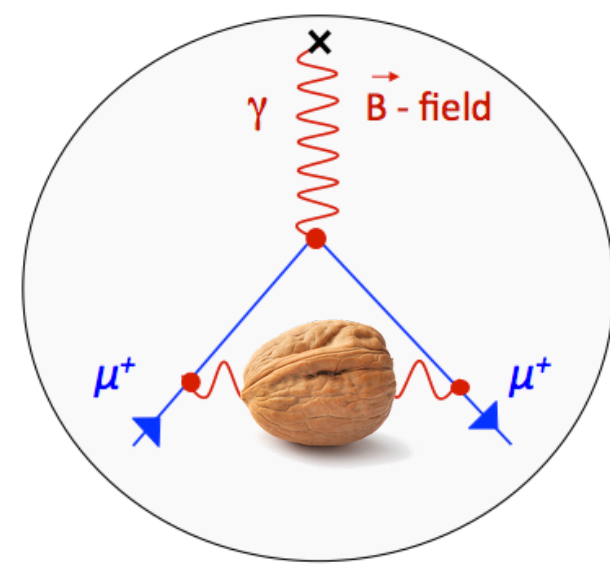
$(g-2)_\mu$: The SM in a Nutshell

$$a_\mu^{SM} = (g_\mu - 2)/2 = a_\mu^{QED} + a_\mu^{weak} + a_\mu^{had}$$

↑
gyromagnetic factor of the muon



$(g-2)_\mu$: The SM in a Nutshell



$$a_\mu^{SM} = (g_\mu - 2)/2 = a_\mu^{QED} + a_\mu^{weak} + a_\mu^{had}$$

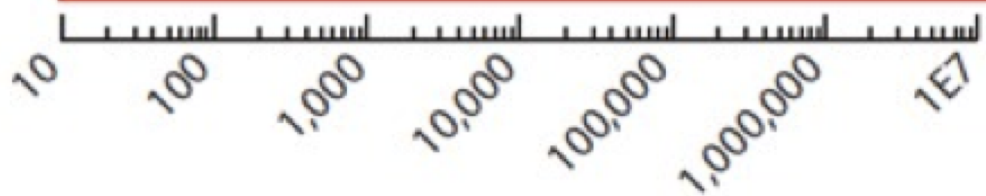
Brookhaven 2004 $\left(\frac{\alpha}{\pi}\right)^4$ + Hadronic + Weak

CERN III 1979 $\left(\frac{\alpha}{\pi}\right)^3$ + Hadronic

CERN II 1968 $\left(\frac{\alpha}{\pi}\right)^3$

CERN I 1962 $\left(\frac{\alpha}{\pi}\right)^2$

Nevis 1960 $\frac{\alpha}{2\pi}$



Uncertainty of measurement in 10^{-11}



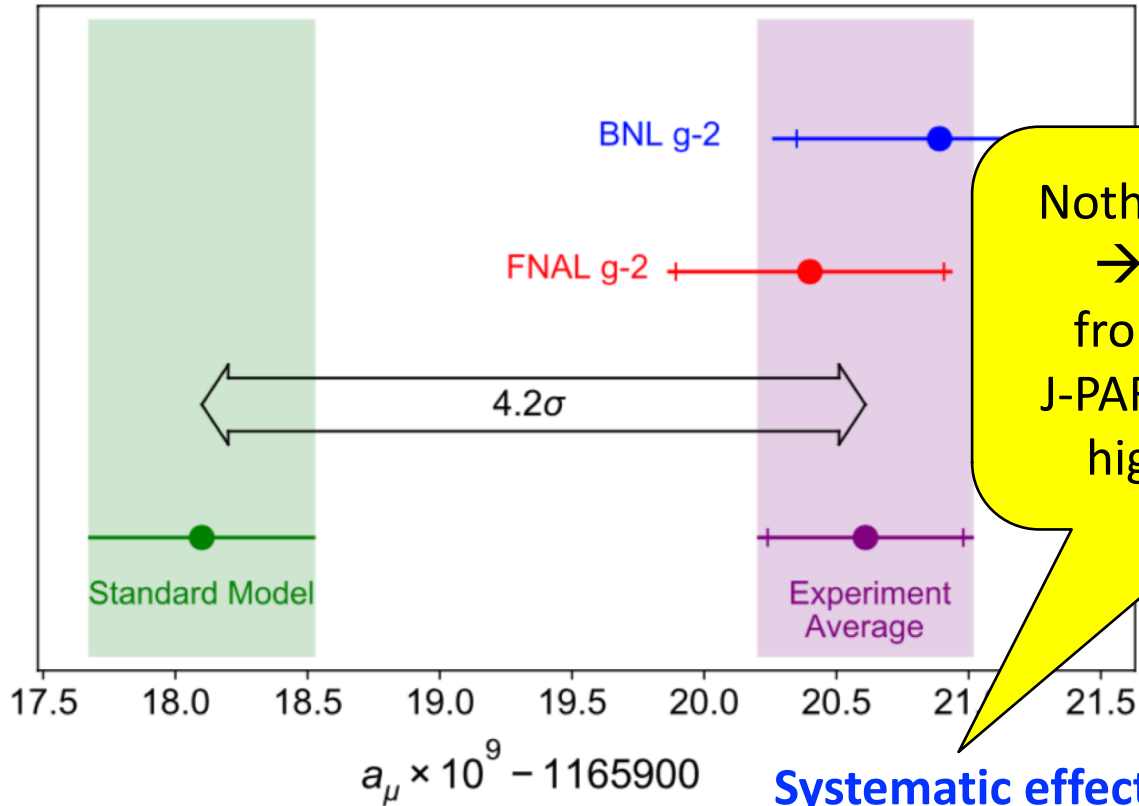
FNAL

CERN I



New direct $(g-2)_\mu$ Measurement FNAL

Strong indication for physics beyond the SM ?!



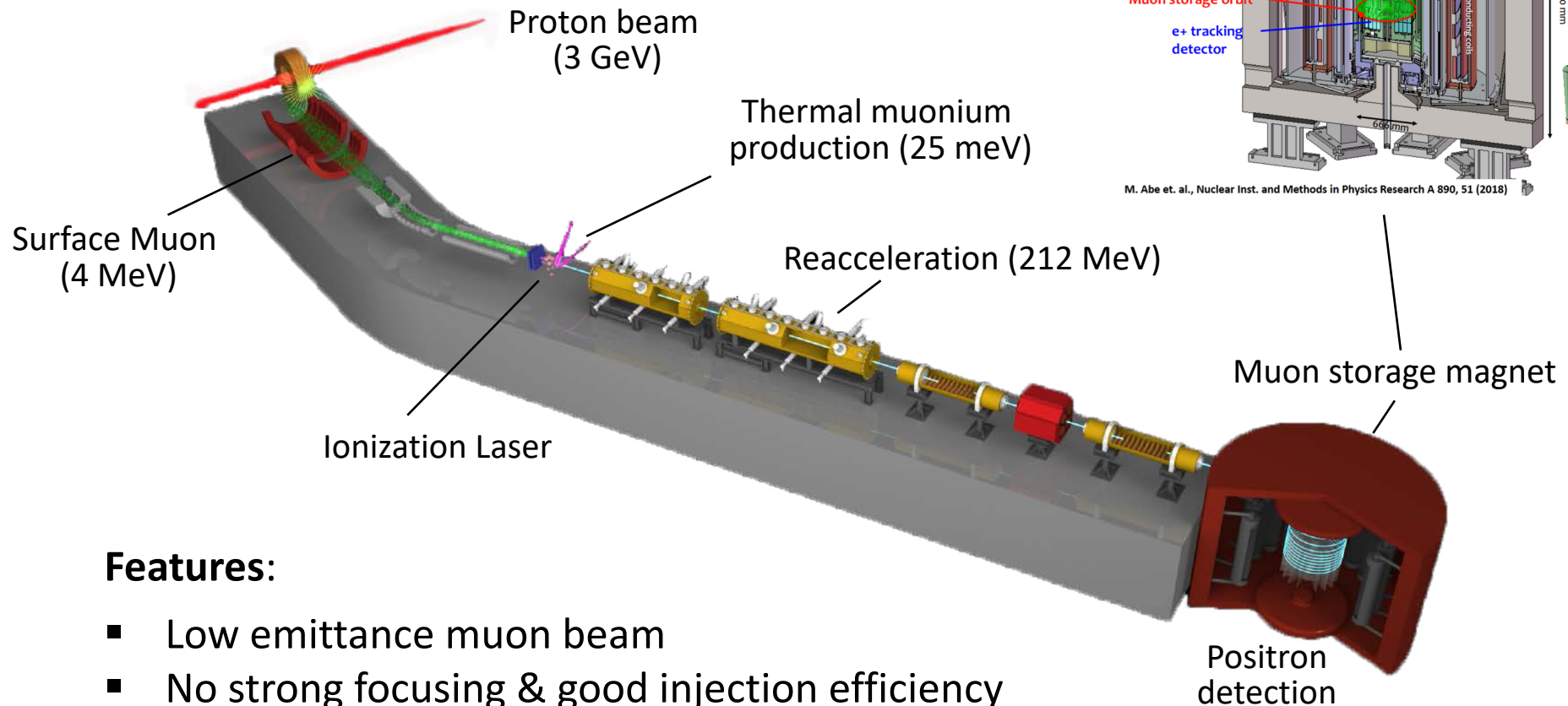
Nothing found so far,
 → confirmation
 from independent
 J-PARC measurement
 highly desirable !

**Systematic effect in
 BNL/FNAL method ?**



Meson2021
 Dinko Pocanic

J-PARC g-2 Experiment (2024+)

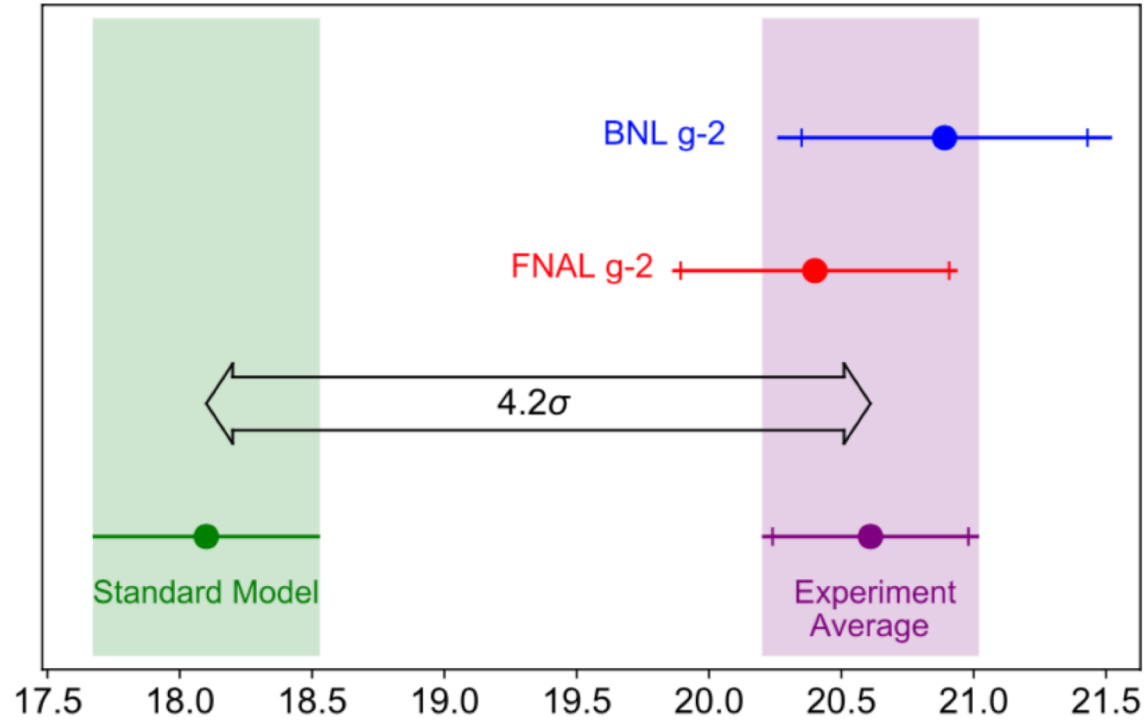


Features:

- Low emittance muon beam
 - No strong focusing & good injection efficiency
 - Compact storage ring
 - Tracking detectors with large acceptance
- Completely different from BNL/FNAL method

New direct $(g-2)_\mu$ Measurement FNAL

Strong indication for physics beyond the SM ?!



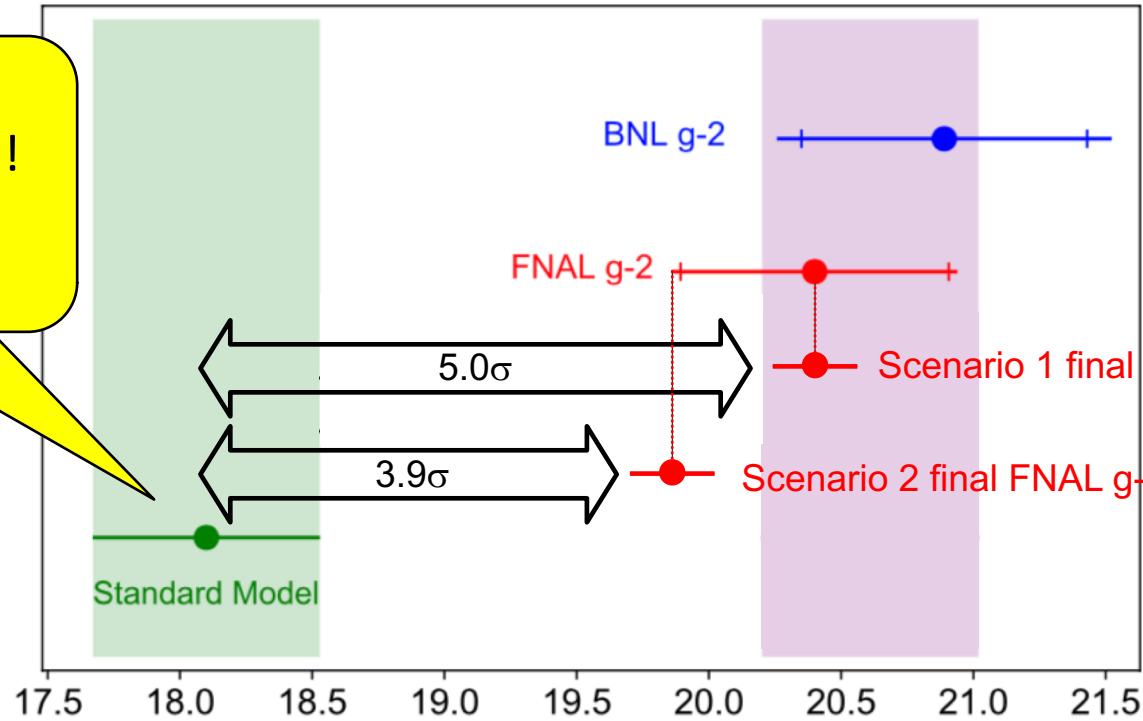
How stable is the SM prediction ?



New direct $(g-2)_\mu$ Measurement FNAL

Strong indication for physics beyond the SM ?!

Reduction of SM prediction needed!
 → Impact from Meson Physics !



How stable is the SM prediction ?
 $a_\mu \times 10^9 - 1165900$



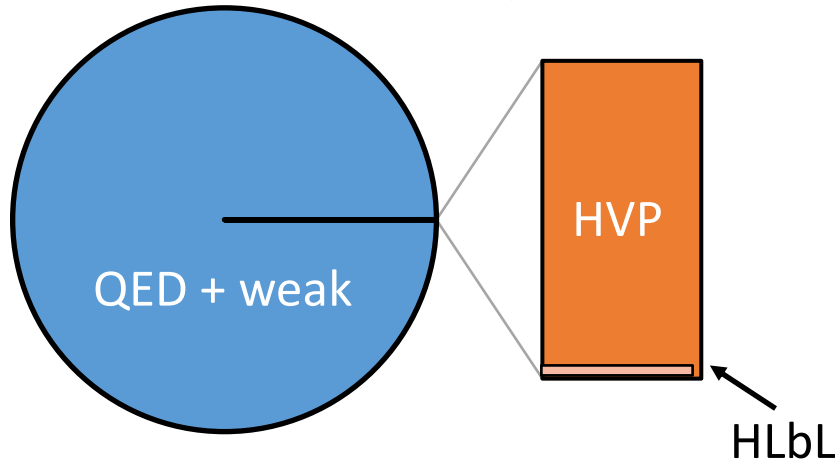
Standard Model Prediction of $(g-2)_\mu$

$$a_\mu^{SM} = a_\mu^{QED} + a_\mu^{weak} + a_\mu^{had} = (11\,659\,181.0 \pm 4.3) \cdot 10^{-10}$$

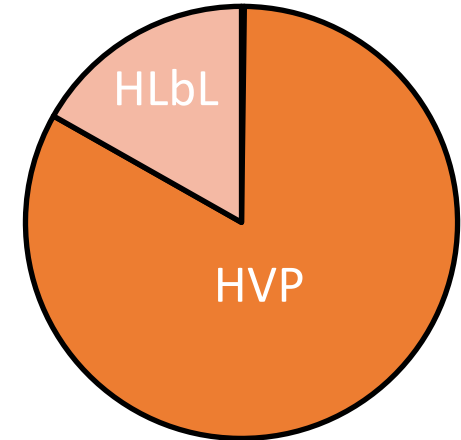
Kinoshita et al. '12
 $(11\,658\,471.808 \pm 0.015) \cdot 10^{-10}$

Czarnecki et al.
 $(15.4 \pm 0.2) \cdot 10^{-10}$

Absolute contribution



(Error contribution)²



The **absolute value of the SM** prediction to muon $(g-2)$ is dominated by **QED** !
 The **error to the SM** prediction to muon $(g-2)$ is dominated by the **hadronic contribution**, where both HVP and HLbL are of relevance !

2019: Standard Model Prediction of $(g-2)_\mu$

Hadronic contribution **non-perturbative**, the **limiting** contribution

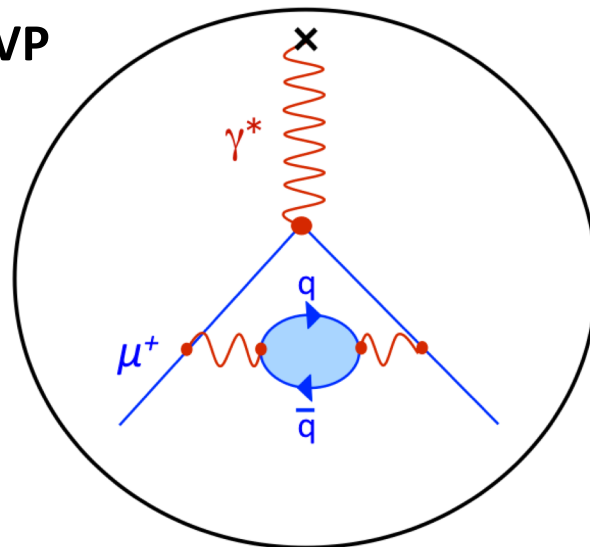
$$a_\mu^{SM} = a_\mu^{QED} + a_\mu^{weak} + a_\mu^{had}$$

→ **HVP**: Hadronic Vacuum Polarization ($\cong 687 \dots 694 \pm 2.4 \dots 4.1$) $\cdot 10^{-10}$

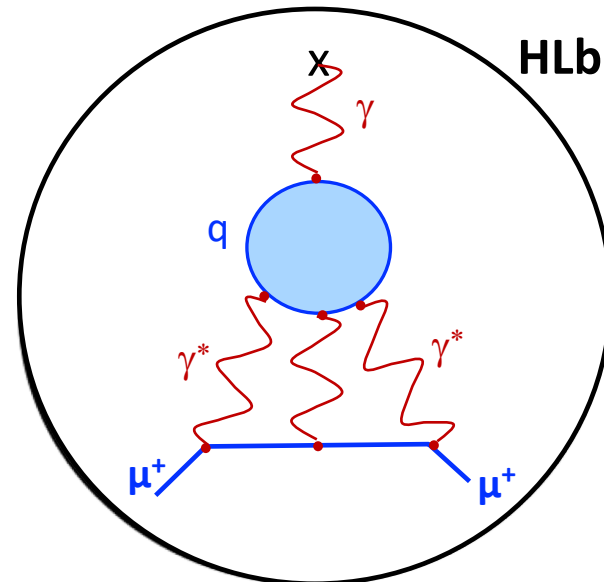
	BDJ19	DHMZ19	FJ17	KNT19
$a_\mu^{HVP, LO} \times 10^{10}$	687.1(3.0)	694.0(4.0)	688.1(4.1)	692.8(2.4)

→ **HLbL**: Hadronic Light-by-Light (10.5 ± 2.6) $\cdot 10^{-10}$ Glasgow „consensus“ value

HVP



HLbL



$(g-2)_\mu$ Theory Initiative

FERMILAB-PUB-20-207-T
INT-PUB-20-021
KEK Preprint 2020-5
MITP 20-028

CERN-TH-2020-075
IFT-UAM/CSIC-20-74
LMU-ASC 18/20
LTH 1234
LU TP 20-20
MAN/HEP/2020/003
PSI-PR-20-06
UWThPh 2020-14
ZU-TH 18/20

196 pages, 103 figures

Goal:
theory consensus value of
muon $g-2$ SM prediction

The anomalous magnetic moment of the muon in the Standard Model

T. Aoyama^{1,2,3}, N. Asmussen⁴, M. Benayoun⁵, J. Bijnens⁶, T. Blum^{7,8}, M. Bruno⁹, I. Caprini¹⁰,
C. M. Carloni Calame¹¹, M. Cè^{9,12,13}, G. Colangelo¹⁴, F. Ciurciello^{15,16}, H. Czyz¹⁷, I. Danilkin¹², M. Davier¹⁸,
C. T. H. Davies¹⁹, M. Della Morte²⁰, S. I. Eidelman^{21,22}, A. X. El-Khadra^{23,24}, A. Gérardin²⁵, D. Giusti^{26,27},
M. Götzmann²⁸, Steven Gottlieb²⁹, V. Gupta³⁰, F. Hagelstein¹⁴, M. Hayakawa^{31,32}, G. Herdozia³², D. W. Hertzog³³,
A. Hoecker³⁴, M. Hoferichter^{43,35}, B.-L. Hoid³⁶, R. J. Hudspith^{12,37}, P. Ignatov³⁷, T. Izubuchi^{37,38}, F. Jegerlehner³⁹,
L. Jin³⁹, A. Keshavarzi³⁹, T. Kinoshita^{40,41}, B. Kubis³⁹, A. Kupich⁴¹, A. Kupsc^{42,43}, L. Laub¹⁴, C. Lehner^{26,27},
L. Lellouch²⁵, I. Logashenko²⁵, B. Malaescu⁴⁴, K. Maitama^{44,45}, M. K. Marinkovic^{46,47}, P. Masjuan^{48,49},
A. S. Meyer²⁷, H. B. Meyer^{12,33}, T. Mibe¹, K. Miura^{12,33}, S. E. Müller⁵⁰, M. Nio^{2,51}, D. Nomura^{52,53}, A. Nyffeler¹²,
V. Pascalutsa¹², M. Passera⁵⁴, E. Perez del Rio⁵⁵, S. Peris^{48,49}, A. Portelli³⁰, M. Procura⁵⁶, C. F. Redmer¹²,
B. L. Roberts⁵⁷, P. Sánchez-Puertas⁵⁸, S. Seddnyakov²¹, B. Shwartz²¹, S. Simula²⁷, D. Stöckinger⁵⁸,
H. Stockinger-Kim⁵⁹, P. Stoffer⁶⁰, R. Van de Water⁶¹, M. Vanderhaeghe^{12,13}, G. Venanzoni⁶¹,
G. von Hippel¹², H. Wittig^{12,13}, Z. Zhang¹⁸,
M. N. Achasov²¹, A. Bashir⁶², N. Cardoso⁶³, B. Chakraborty⁶³, E.-H. Chao¹², J. Charles²⁵, A. Crivellin^{64,65},
O. Deineka¹², A. Denig^{12,13}, C. DeTar⁶⁶, C. A. Dominguez⁶⁷, A. E. Dorokhov⁶⁸, V. P. Druzhinin²¹, G. Eichmann^{69,67},
M. Fael⁷⁰, C. S. Fischer⁷¹, E. Gámiz⁷², Z. Gelzer⁷³, J. R. Green⁷⁴, S. Guellati-Khelifa⁷³, D. Hatton¹⁹,
N. Hermansson-Truedsson¹⁴, S. Holz³⁶, B. Hörz²⁴, M. Knecht²⁹, J. Koponen¹, A. S. Kronfeld²⁴, J. Laiho⁷⁵,
S. Leupold⁶², P. B. Mackenzie¹⁴, W. J. Marciano³⁷, C. McNeile³⁷, D. Mohler^{23,33}, J. Monnard¹⁴, E. T. Neil⁷⁶,
A. V. Nesterenko⁶⁸, K. Ottnad⁷⁷, V. Pauk¹², A. E. Radhabov⁷⁸, E. de Rafael¹, K. Raya⁷⁹, A. Risch¹,
A. Rodríguez-Sánchez⁸⁰, P. Roug⁸⁰, T. San Jose^{12,13}, E. P. Solodov²¹, R. Suga⁸¹, K. Yu. Todyshin⁸², A. Vainshteyn⁸²,
A. Vaquero Avilés-Casco⁸⁶, E. Weil⁷¹, J. Wilhelm¹², R. Williams⁷¹, A. S. Zhevlakov⁷⁸

- Working groups on HVP, HLbL, LatticeQCD, ...
- Three collaboration meetings and various workshops on subtopics
- Scrutiny of various theoretical evaluations
- One consensus value both for HVP and for HLbL

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2006.04822 [hep-ph] 8 Jun 2020



FNAL 2017



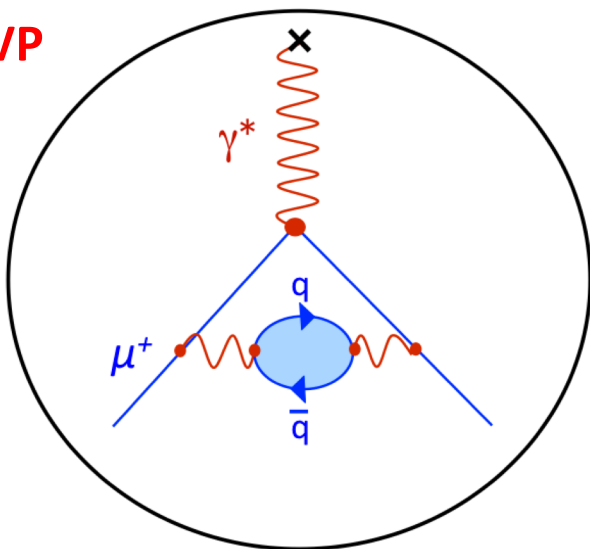
Mainz 2018



Seattle 2019

Hadronic Vacuum Polarization (HVP)

HVP



Estimate of (g-2) Theory Initiative
based on dispersive approach
(including higher orders):

$$(693.1 \pm 4.0) \cdot 10^{-10}$$

was ($\cong 687 \dots 694 \pm 2.4 \dots 4.1$) $\cdot 10^{-10}$

see also Meson2021
Bastian Kubis
Pere Masjuan

Hadronic Vacuum Polarization Contrib. to $(g-2)_\mu$

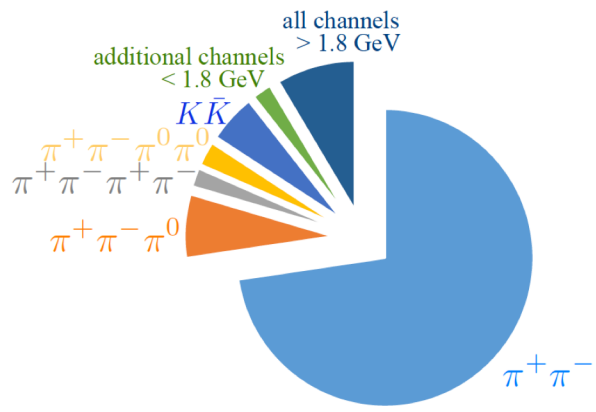
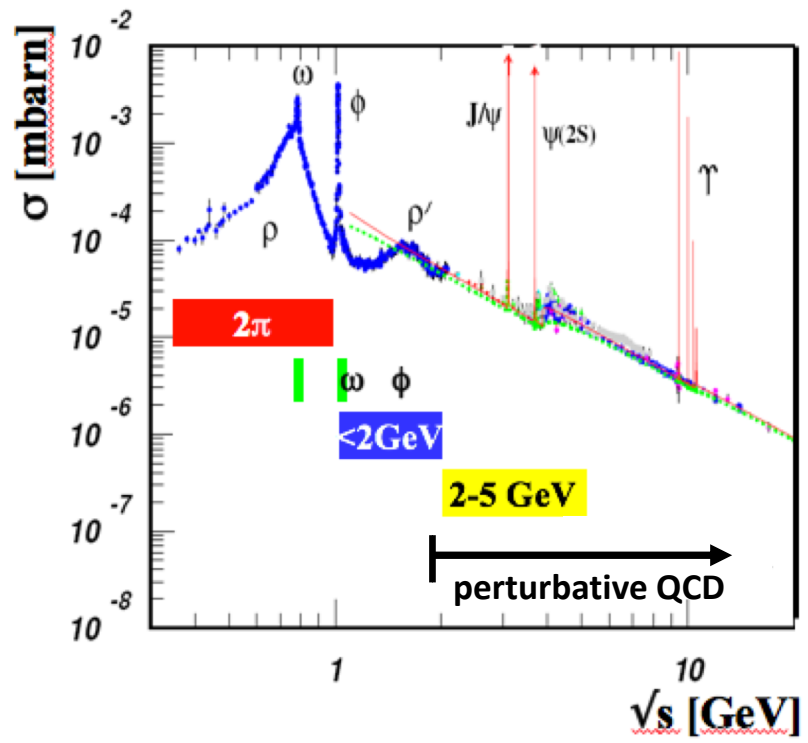
Optical theorem (unitarity) and analyticity:

Data-driven approach: $K(s)$: known kernel function
 s : energy²

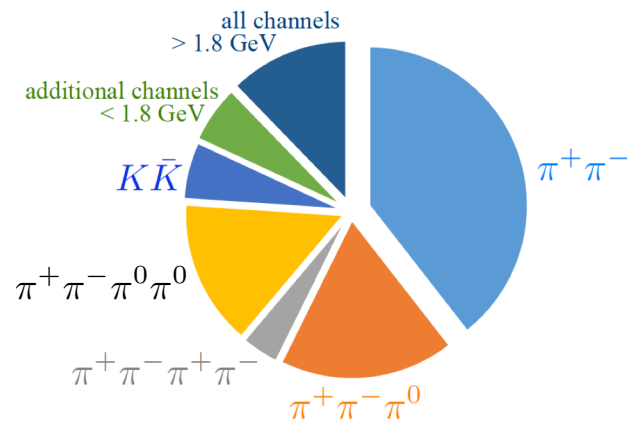
$$a_\mu^{HVP} = \frac{1}{4\pi^3} \int_{4m_\pi^2}^{\infty} ds K(s) \sigma_{had}(s)$$

$$\sigma_{had}(s) = \sigma_{tot}(e^+e^- \rightarrow \text{Hadrons})$$

low energy contributions especially important!



Contributions to HVP integral

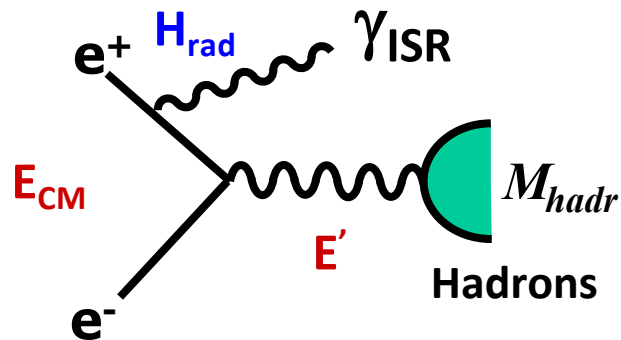


Contributions to HVP error

Status of the $g-2$ problem

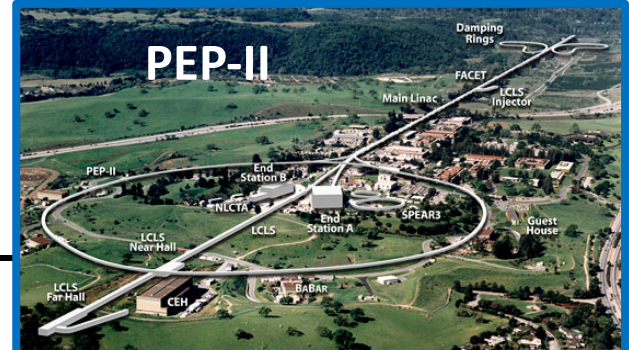
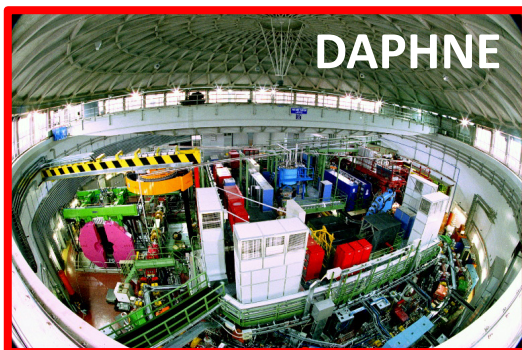
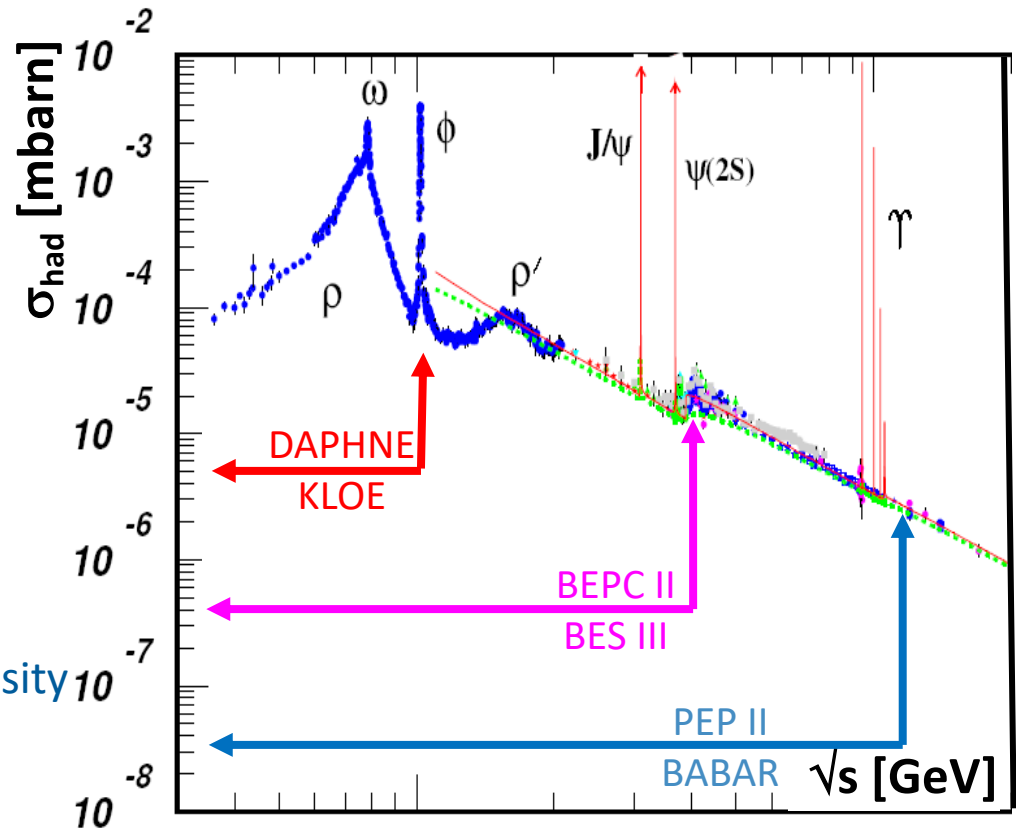
Initial State Radiation (ISR)

Initial State Radiation (ISR) aka Radiative Return

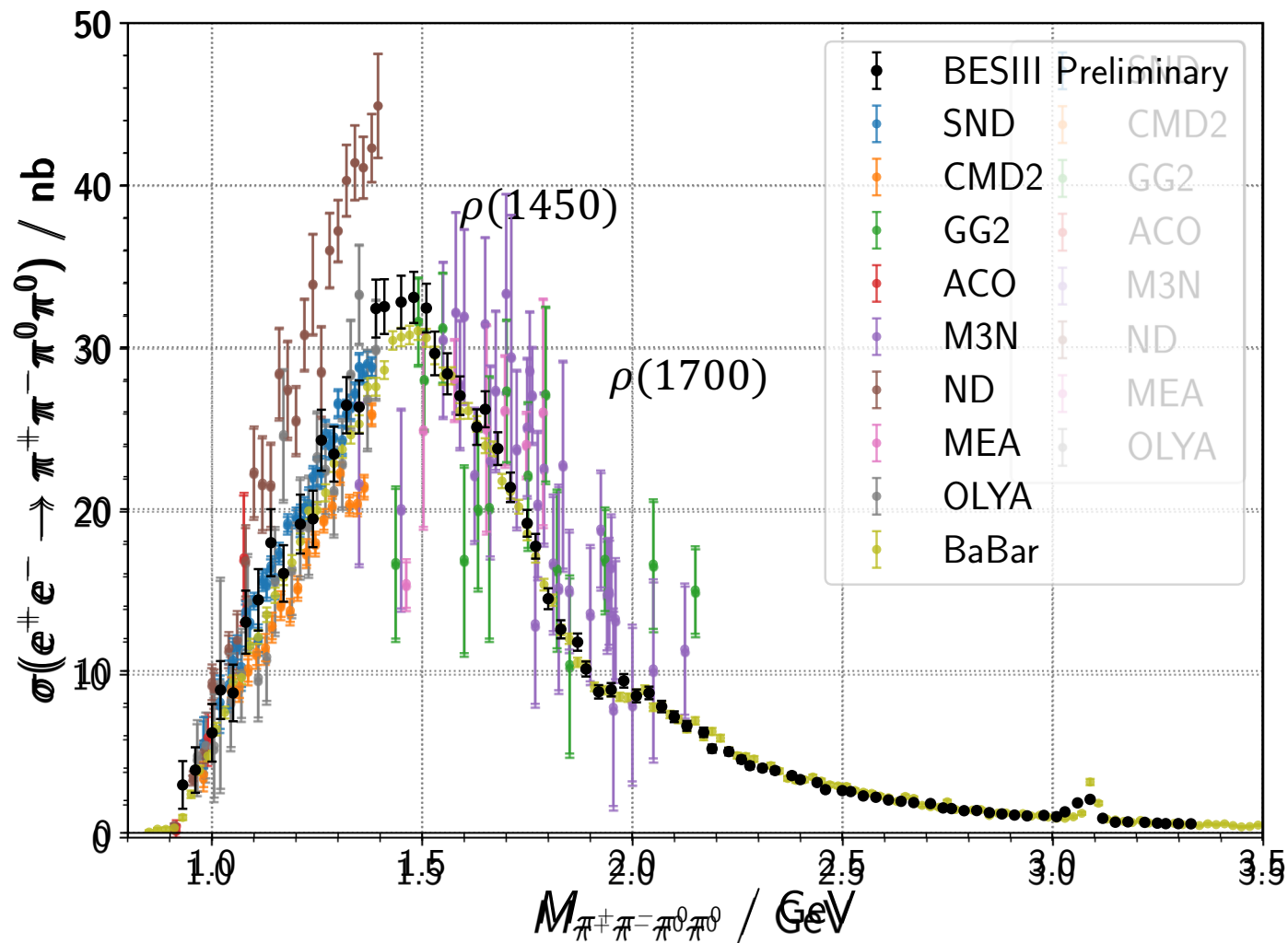


- No systematic variation of E_{beam}
- High statistics thanks to high luminosity
- Precise knowledge of radiative corrections mandatory (H_{rad})

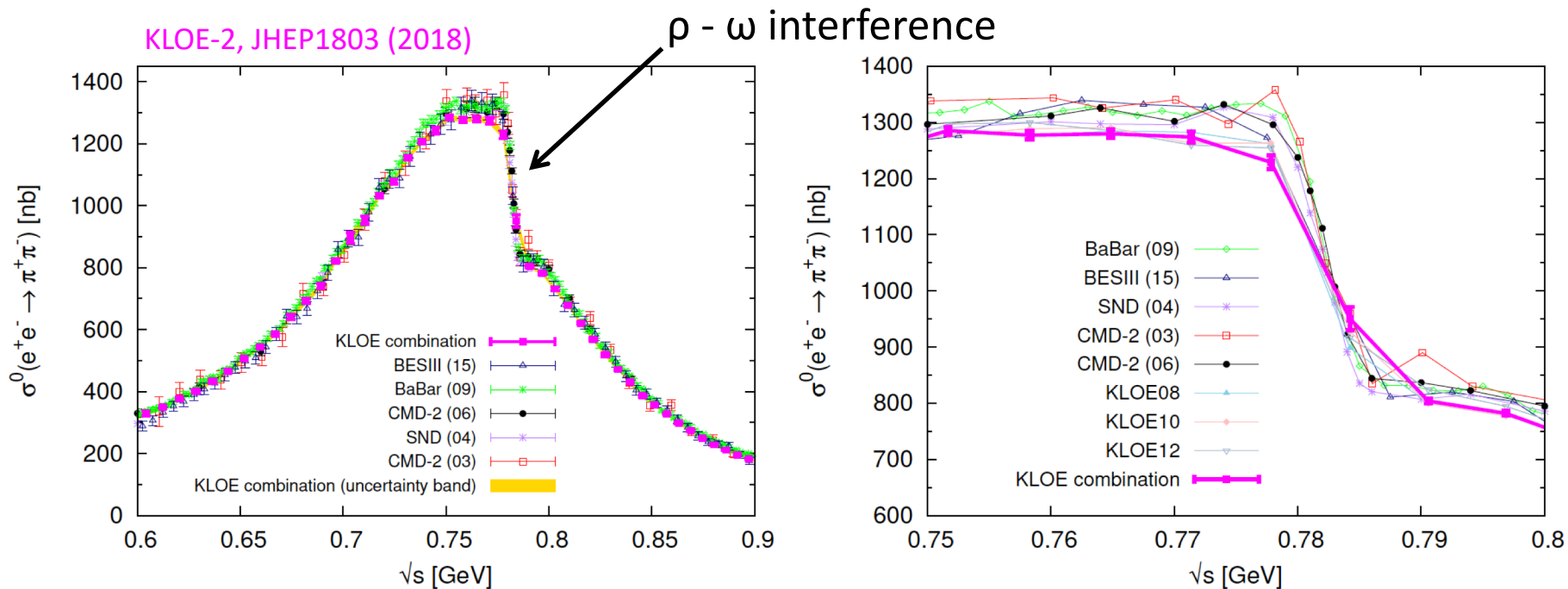
PHOKHARA event generator



ISR (BABAR & BESIII): $e^+e^- \rightarrow \pi^+\pi^-\pi^0\pi^0$



Most relevant Channel: $e^+e^- \rightarrow \pi^+\pi^-$



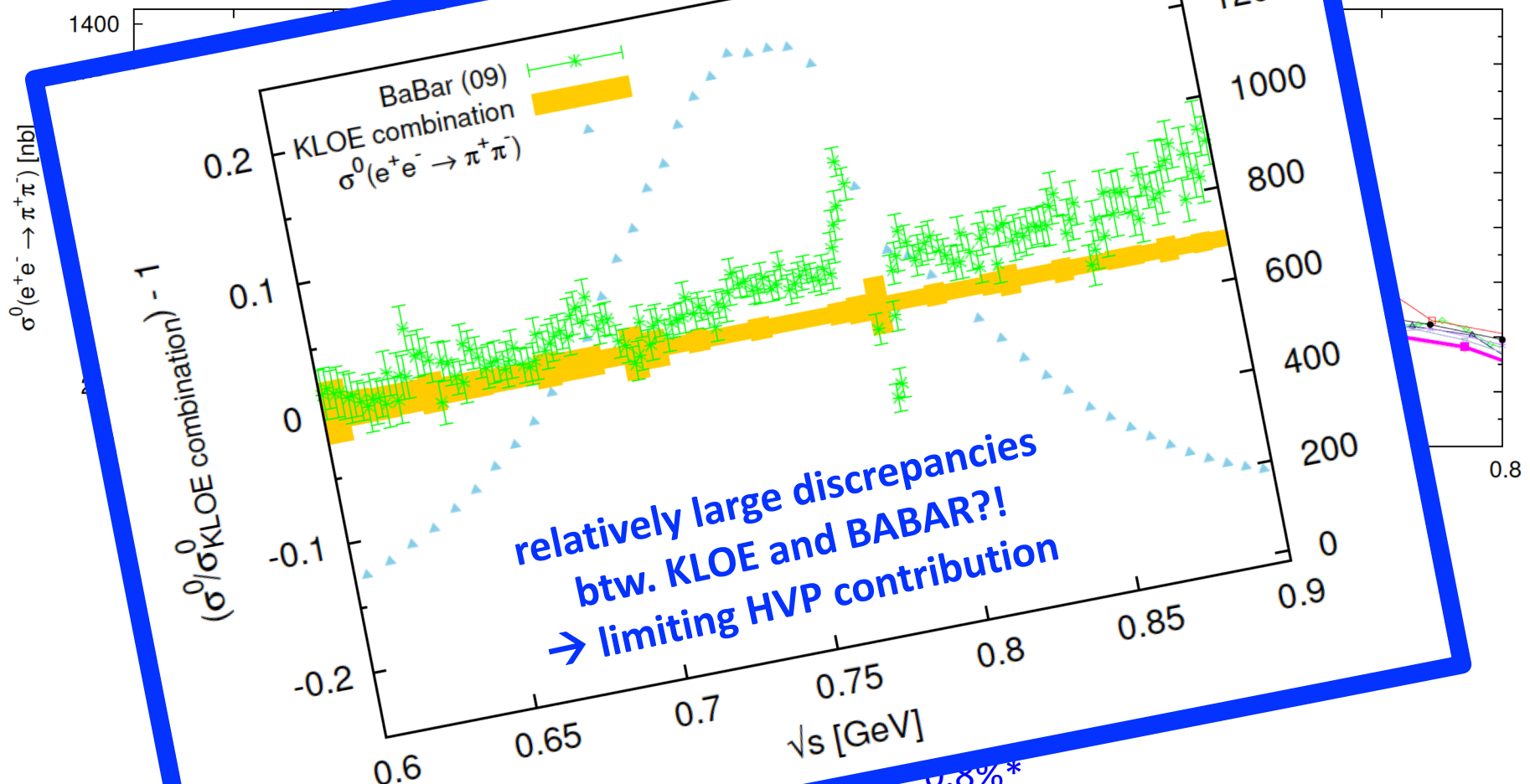
Systematic Uncertainties on $\rho(770)$ peak

- ISR BABAR 0.5%
- ISR KLOE 0.6% (average of 3 analyses)
- ISR BESIII 0.9%
- Energy Scan CMD2 0.8%*
- Energy Scan SND 1.5%*

* limited in addition by statistics

Most relevant Channel: e^+e^-

KLOE-2, JHEP1803 (2018)

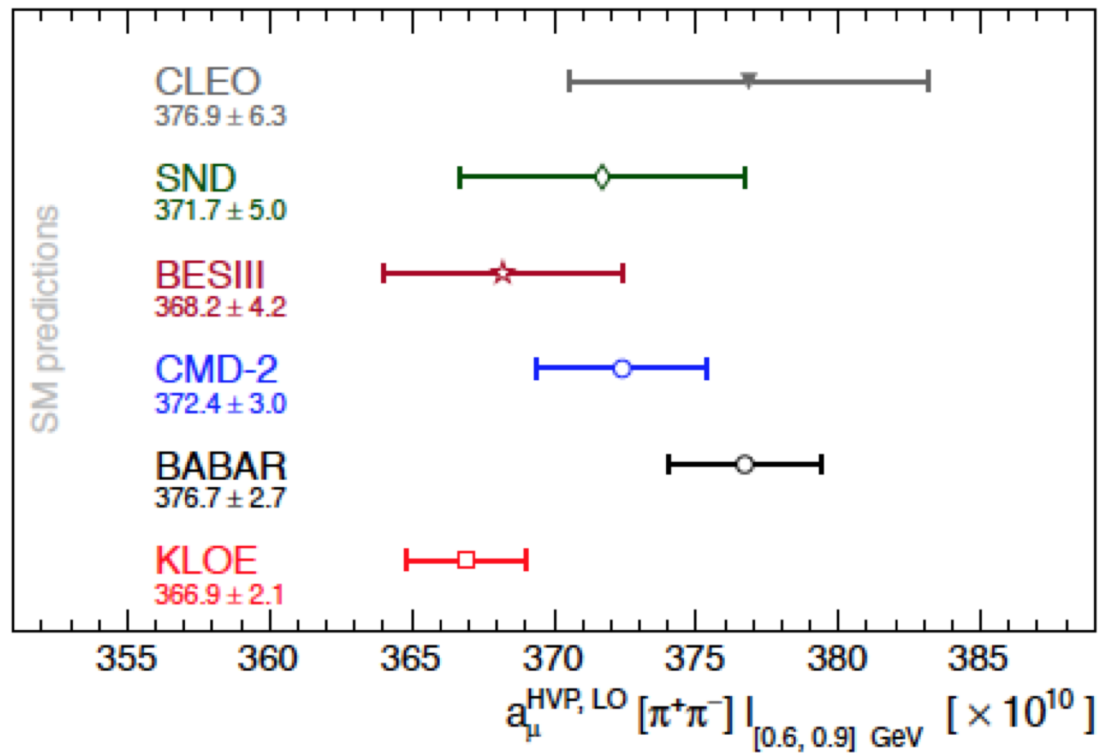


by scan SND 0.8%* 1.5%*

* limited in addition by statistics

Most relevant Channel: $e^+e^- \rightarrow \pi^+\pi^-$

2π contribution to HVP contribution to $g-2$ (600 – 900 MeV)



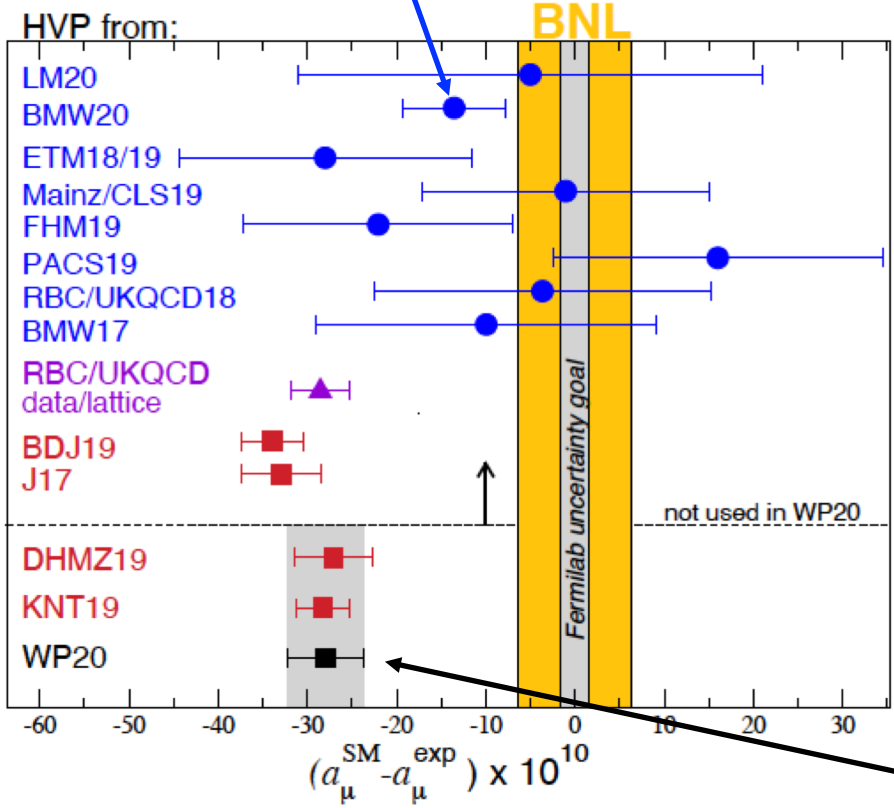
Conclusions & Outlook HVP

- HVP error (and therefore SM prediction of muon g-2) largely limited by KLOE– BABAR discrepancy of the pion FF measurement
 - Existing BESIII and SND measurements (0.9%, 0.8% error) not yet precise enough to rule out either KLOE or BABAR
 - New ISR measurements expected from BABAR, BESIII, BELLE-II: Try to push systematic uncertainties down to 0.5% or better
 - High statistics energy scans from VEPP-2000/Novosibirsk (CMD-3, SND): Expect similar accuracy Meson2021: Alexander Obrazovsky
 - Better accuracy from higher multiplicity states and R_{incl} (KEDR, BESIII)
- Assuming agreement among new BABAR, BESIII, BELLE-II, CMD-3, KLOE and individual accuracies on the 0.5% level (or eventually better)

REDUCTION OF UNCERTAINTY OF HVP BY FACTOR OF 2 IN REACH !

Conclusions & Outlook HVP

First LatticeQCD result (BMW) with sub-percent precision
→ needs clarification by other Lattice groups



Ab-initio lattice QCD(+QED) calculations are maturing

Difficult problem: scales from $2m_\pi$ to several GeV enter; cross-checks needed at high precision

Hybrid window method restricts scales that enter from lattice/dispersive data

Dispersive, $e^+e^- \rightarrow$ hadrons (20+ years of experiments)

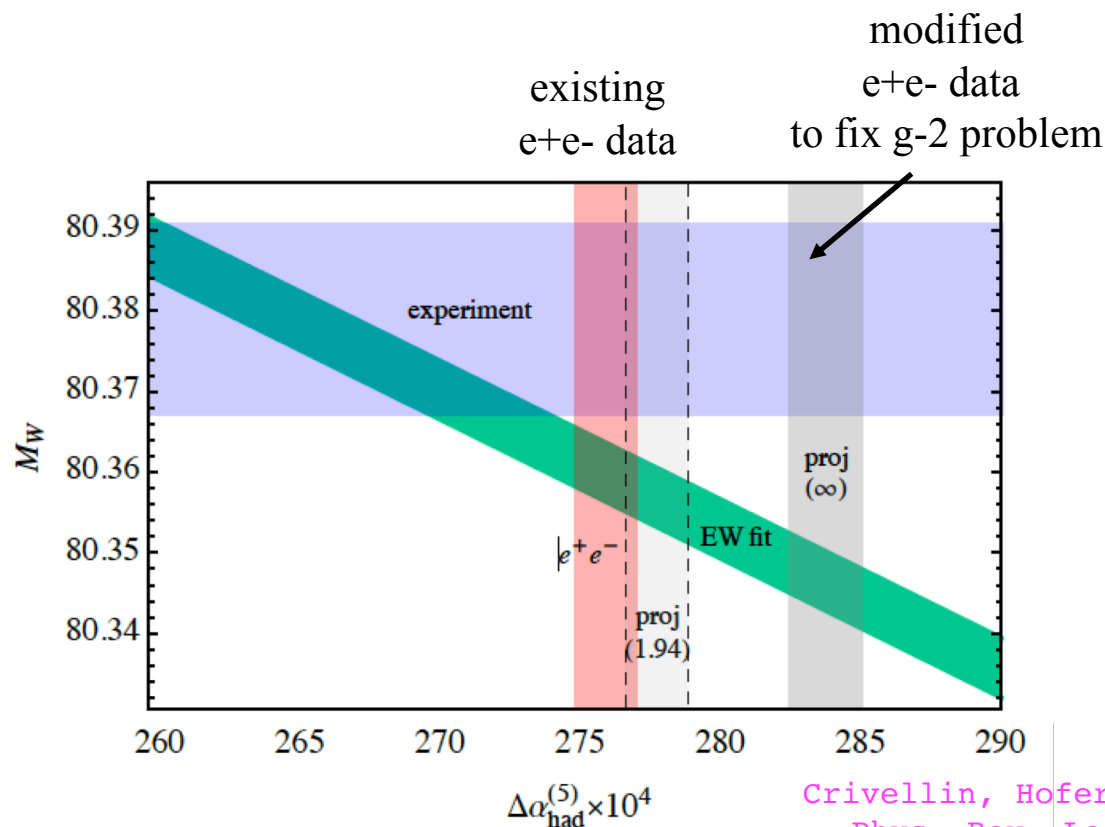
HVP value from g-2 Theory Initiative

HVP and Electroweak Precision Physics

Artificially increasing e^+e^- cross sections (over full energy range) to match a_μ^{exp}

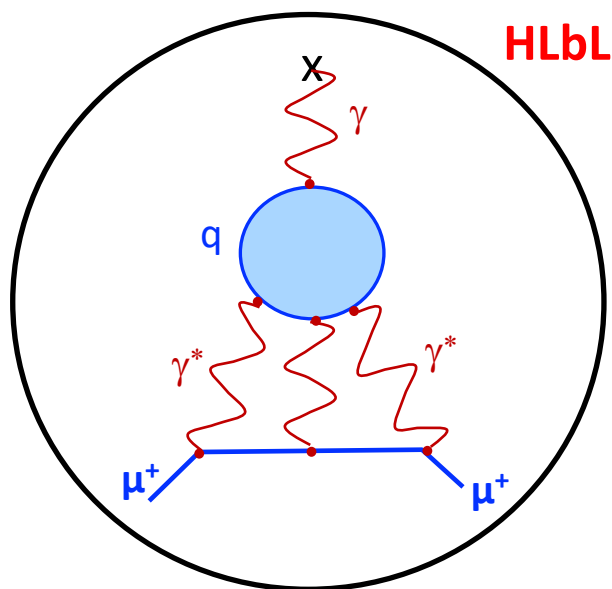
→ Impact on running of fine structure constant $\Delta\alpha_{\text{had}}(M_Z^2)$

→ increasing deviation btw. EW fit and EW measurements (e.g. M_H , M_W , ...) ?!



Crivellin, Hoferichter, Manzari, Montull
Phys. Rev. Lett. 125, 091801 (2020)

Hadronic Light-by-Light Contribution (HLbL)



HLbL

Estimate of (g-2) Theory Initiative:

$$(9.2 \pm 1.8) \cdot 10^{-10}$$

was $(10.5 \pm 2.6) \cdot 10^{-10}$

see also Meson2021
Bastian Kubis
Emilie Passemar

Hadronic Light-by-Light (HLbL)

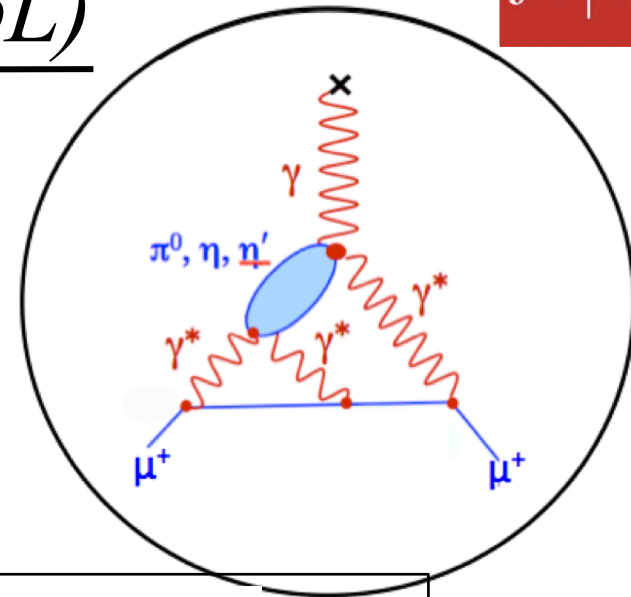
Glasgow consensus value: $(10.5 \pm 2.6) \cdot 10^{-10}$

Prades, de Rafael, Vainshtein '09

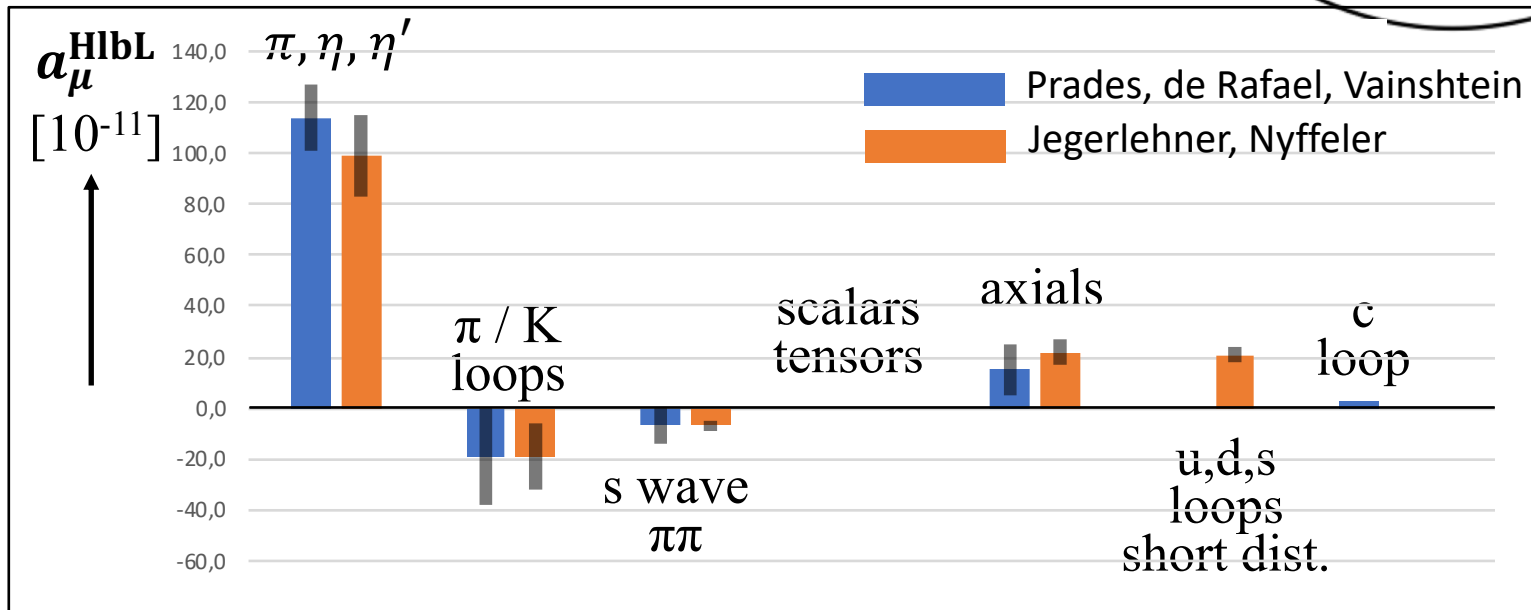
model-dependent!

$(11.6 \pm 3.9) \cdot 10^{-10}$

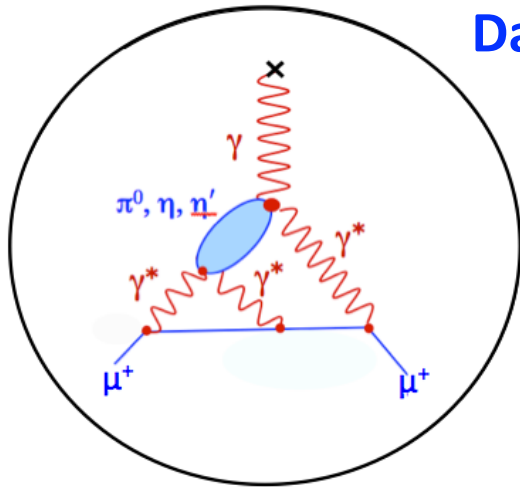
Jegerlehner, Nyffler '09



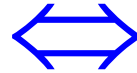
Decomposition in terms of individual contributions:



Data-Driven Approaches (e.g. Pion-Pole)

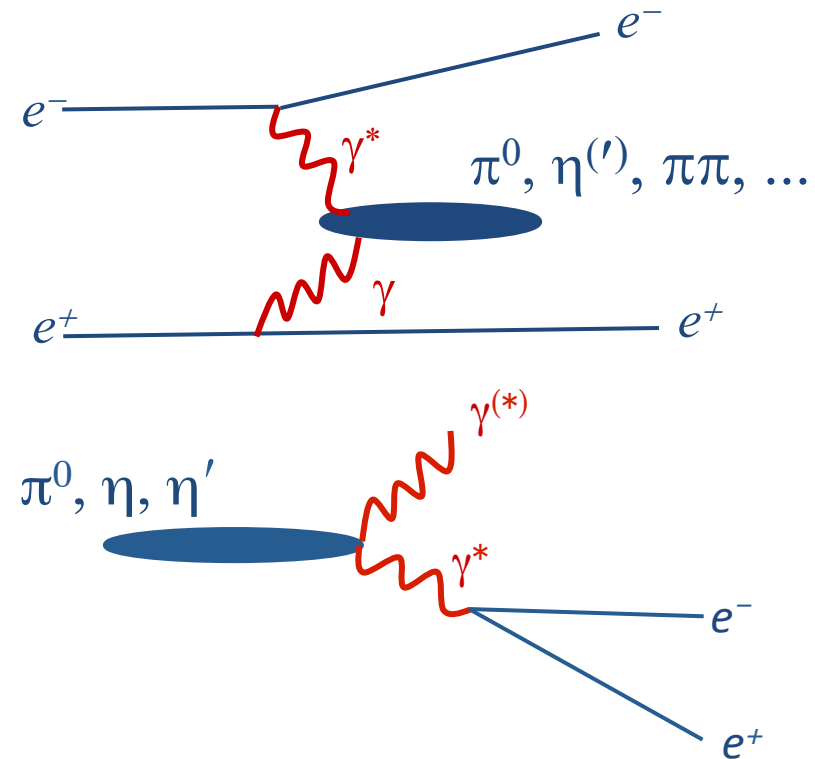


Data-driven approach!



Exp. Input !
Transition

Form Factors $F(Q^2)$
below $\sim 2 \text{ GeV}^2$



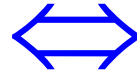
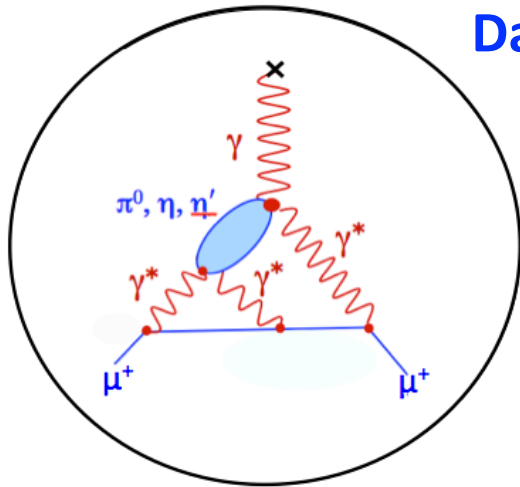
NEW

Dispersion Relations being developed
using experimental measurements
of meson transition form factors!

Colangelo et al '14; Pauk, Vanderhaeghen '14

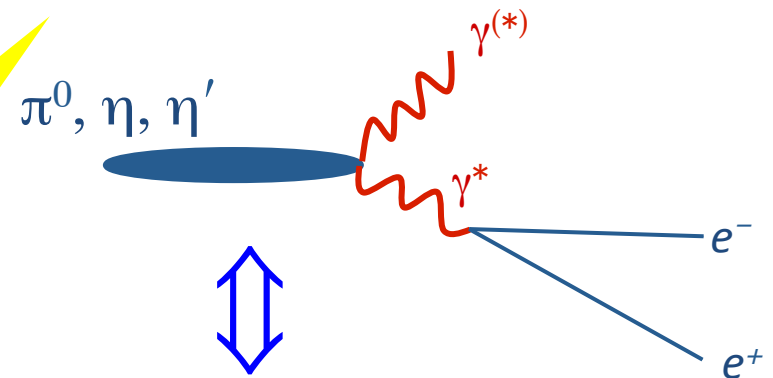
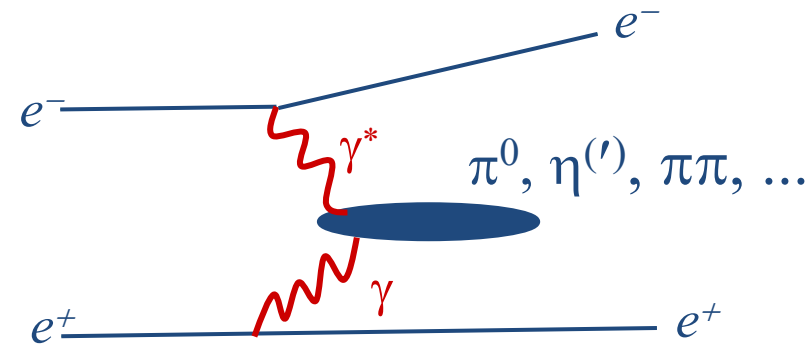
Data-Driven Approaches (e.g. Pion-Pole)

Data-driven approach!



Exp. Input !
Transition

Form Factors $F(Q^2)$
below $\sim 2 \text{ GeV}^2$



NEW

Experimental challenges:

Now: measure single-virtual TFF and compare with theory assumption!

Future: provide measurements of double-virtual TFFs

Problem: double-virtual TFFs needed, for which no measurements exist yet!

Way out: use theory calculations for double-virtual TFFs:

- Lattice QCD calculation
- Dispersive analysis

Spacelike FFs $\gamma\gamma^* \rightarrow P$

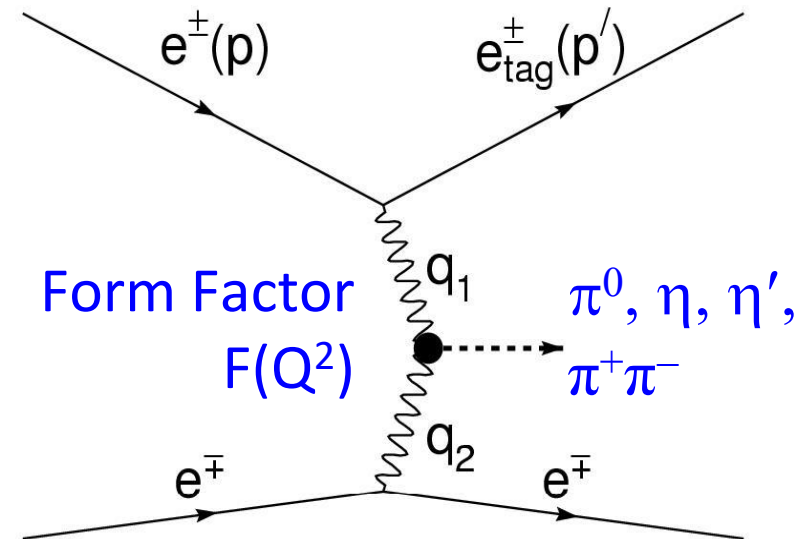
Single Tag Method

Selection criteria

- 1 electron (positron) detected
 - 1 positron (electron) along beam axis
 - Meson fully reconstructed
- **cut on angle of missing momentum**

Momentum transfer

- tagged: $Q^2 = -q_1^2 = -(p - p')^2$
→ Highly virtual photon
- untagged: $q^2 = -q_2^2 \sim 0 \text{ GeV}^2$
→ Quasi-real photon



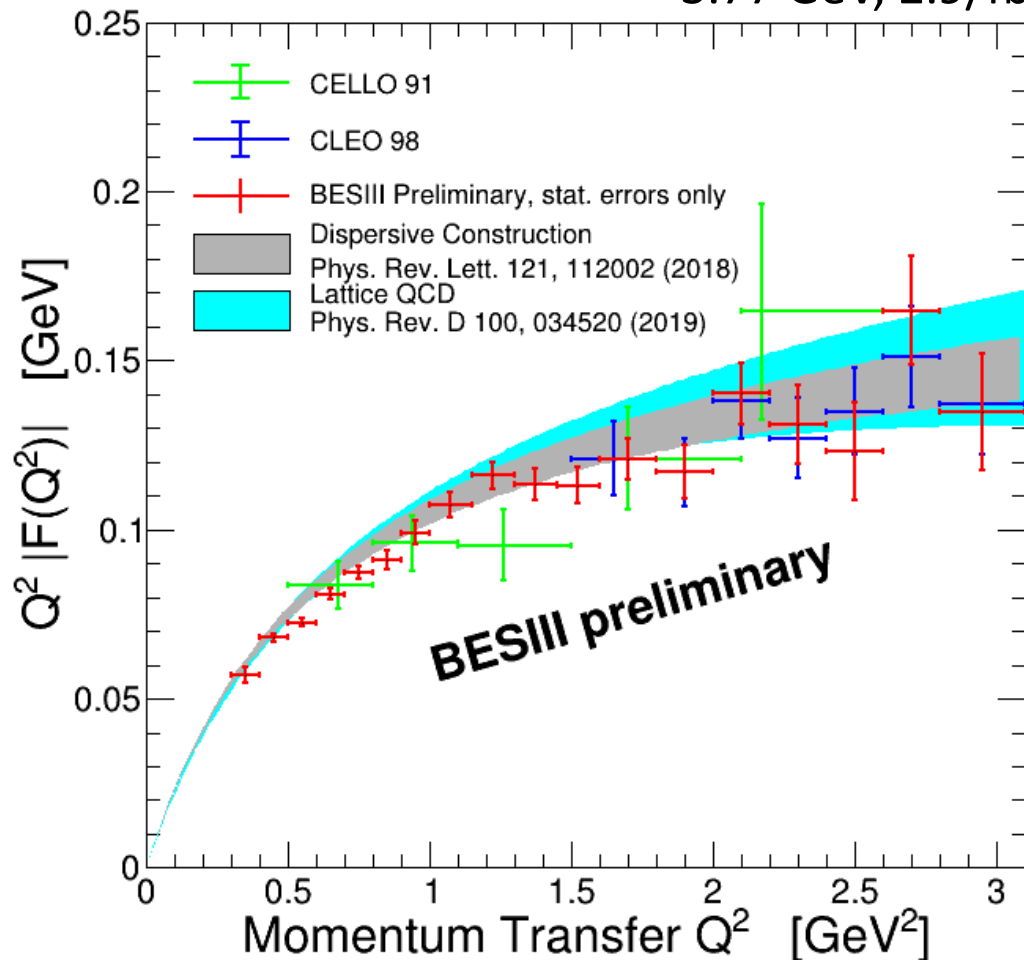
$$Q^2 = 4 \cdot E \cdot E' \cdot \sin^2(\theta/2)$$

EKHARA event generator
Czyż, Ivashyn

BES III Analysis: $\gamma\gamma^* \rightarrow \pi^0$

PPNP107(2019)20

3.77 GeV, 2.9/fb

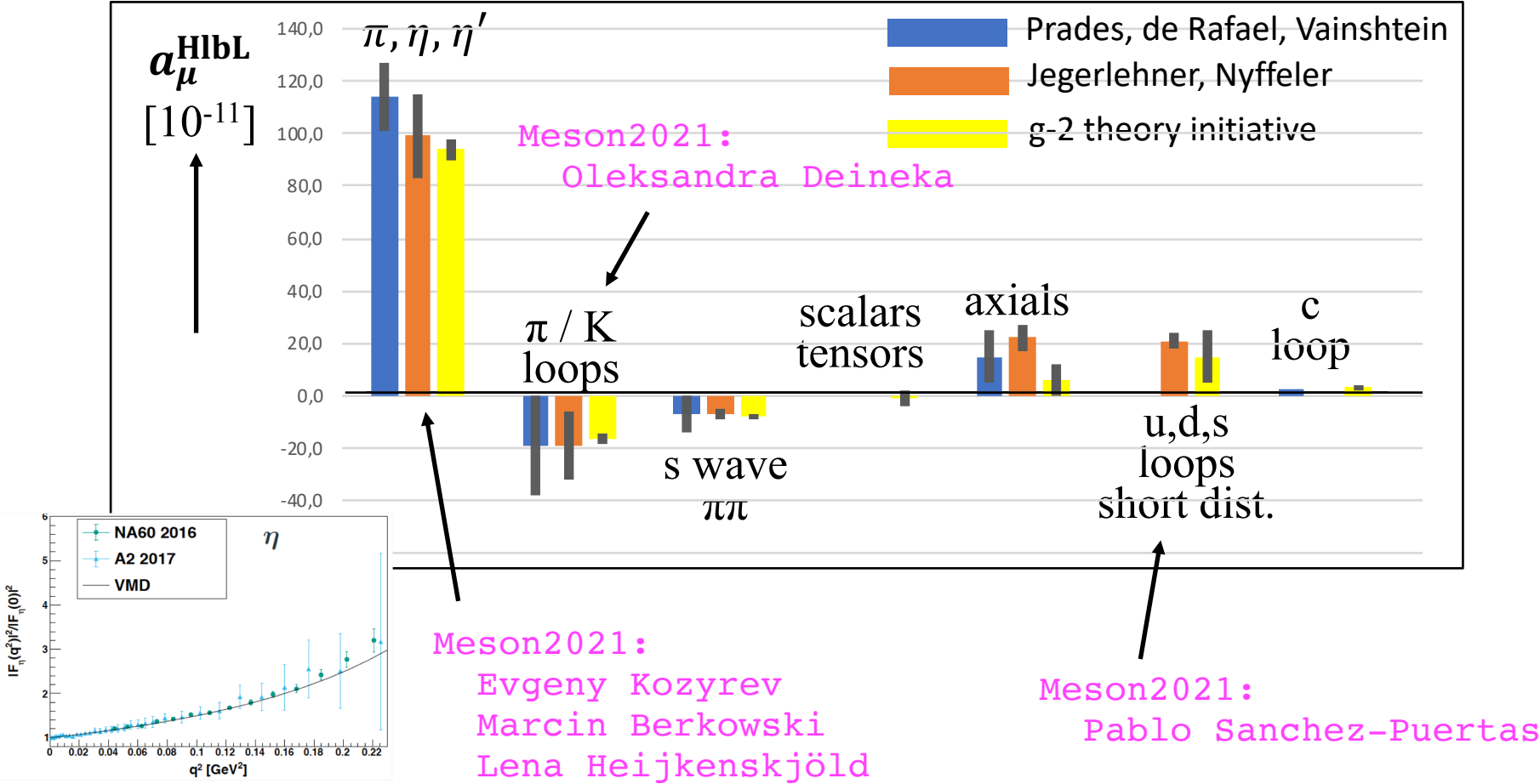


Unprecedented accuracy of BESIII
 Relevant Q^2 range for HLbL
 Very good agreement with recent
 dispersive analysis and of
 Lattice QCD calculation

Q^2 range below 0.3 GeV² accessible
 at BESIII with data from lower
 c.m. energy

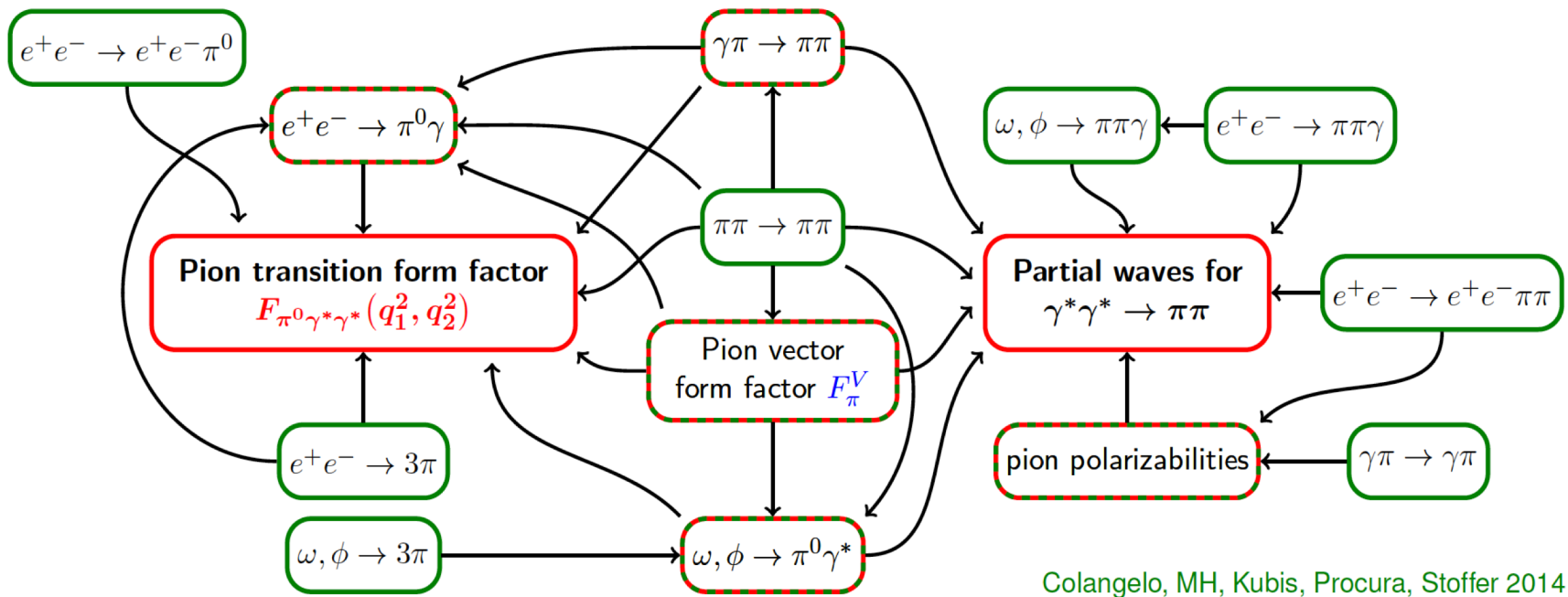
Conclusion & Outlook HLbL

- Theory initiative was able to significantly reduce the HLbL error (data-driven approach) and also inclusion of first Lattice QCD results



Conclusion & Outlook HLbL

- Usage of theoretical tools to relate meson decays & reactions

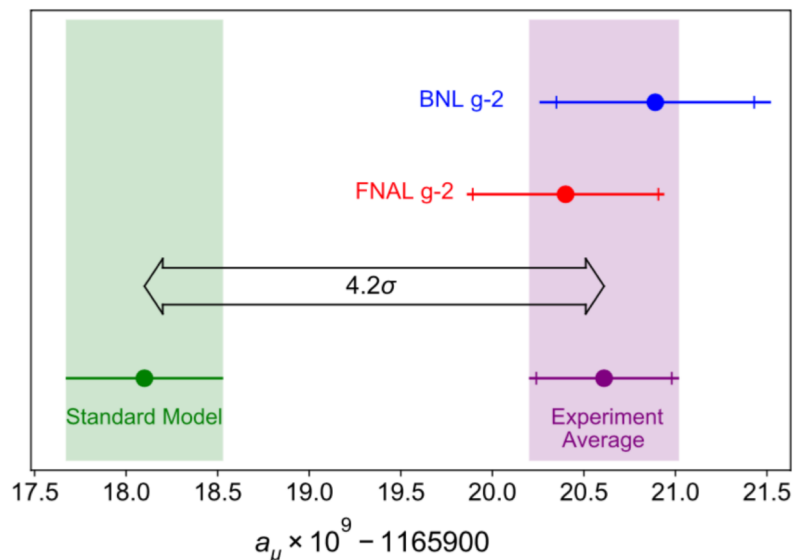


- Dedicated program at various facilities in the world (Europe, US, Asia)



BABAR





Conclusions:
Yes, we have good reasons to be excited!



Conclusions

- 20 year old BNL measurement of $g-2$ confirmed by FNAL 4.2σ discrepancy to SM, J-PARC project upcoming!
- HVP:** By combining new BESIII data on pion FF with KLOE and future data from BELLE II, CMD-3, and re-analysis of BABAR
 → reduction of uncertainty by a factor of 2 in a global effort!
- HLbL:** new generation of transition FF measurements ongoing at various places,
 → further reduction of uncertainty in reach (assume factor 1.5)

Assumption: central value of SM stable and uncertainty will improve to $\pm 2.3 \cdot 10^{-10}$!

Scenario: New experimental value stays constant, factor 4 exptl. improvement

$$\rightarrow \Delta a_\mu = a_\mu^{\text{exp}} - a_\mu^{\text{SM}} = (25.1 \pm 2.7) \cdot 10^{-10} \quad (9.4\sigma) \quad !!!$$

- FF measurements for HVP and HLbL allow for searches for dark photons/ALPS

Meson2021: Attila Krasznahorkay

Conclusions

- 20 year old BNL experiment of a_μ shows 4.2σ discrepancy

- from a_μ
 - \rightarrow real

- HLbL: new \rightarrow

Final interpretation of the muon g-2 crucially depends on Meson Physics research

As \rightarrow Scenario



- FF meson

allow searches for dark photons/ALPS

Meson2021: Attila Krasznahorkay



10^{-10} !

1. improvement

!!!

10

Thank you !

NEW DATE
AUG. 29 TO SEPT. 03, 2021
MAINZ, ERBACHER HOF

INTERNATIONAL PHYSICS SCHOOL
MUON DIPOLE MOMENTS
AND HADRONIC EFFECTS

https://indico.mitp.uni-mainz.de/e/g-2_school

TOPICS AND SPEAKERS

- Muon Magnetic Moment Experiment Gordon Hanson (BNL, USA)
- Muon Magnetic Moment Theory Dariusz Kotus (JYU, Japan)
- Hadronic, Light-by-Light Phenomenology Boris Kubis (Bonn, Germany)
- Data Input to Hadronic Vacuum Polarization SBA at Lucha Roberts, Italy
- Data Input to Hadronic, Light-by-Light Christoph Reuber (Mainz, Germany)
- Particle Detectors Wolfgang Kohn (Gothen, Germany)
- Lattice QCD Theory Martin Hasenbusch (Duisburg, Germany)
- New Physics Contributions to $g-2$ Saptarshi Ghosh (Stony Brook, USA)
- Atomic Physics Precision Experiments Klaus Blaum (MPI Heidelberg, Germany)
- Exotic Neutrons Lisa Heppner (GSI Mainz, Germany)

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Logos: PRISMA, SFB, WILHELM UND ELSA HERAULUS-STIFTUNG, GUTENBERG-UNIVERSITÄT, KJL

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